

The art of light control & precision measurement

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ICAP Summer School, Paris, July 19, 2012



A modern epoch in quantum metrology

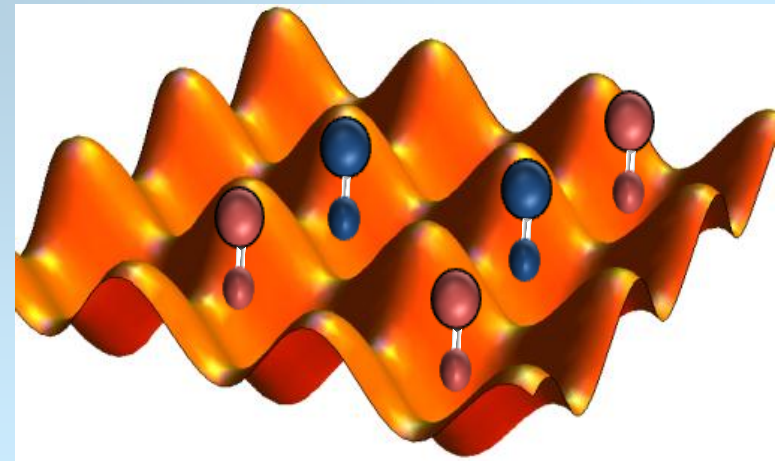
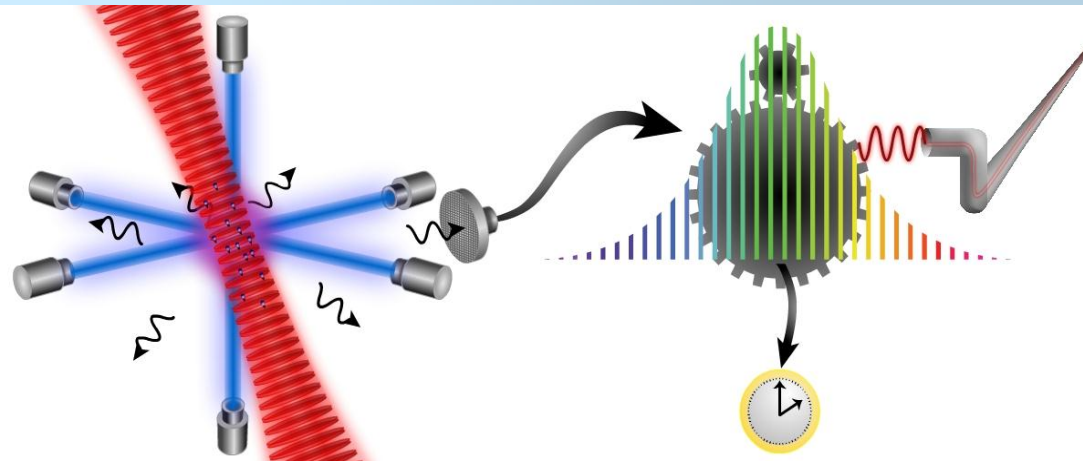
Precision
Measurement



Many-particle
Quantum systems

Many-body physics & novel quantum states push the fundamental limit of measurement

Precision measurement & clocks determine microscopic parameters and system properties



Lecture I: Art of light control

Lecture II: Precision quantum metrology

Lecture III: Ultracold molecules - a new frontier

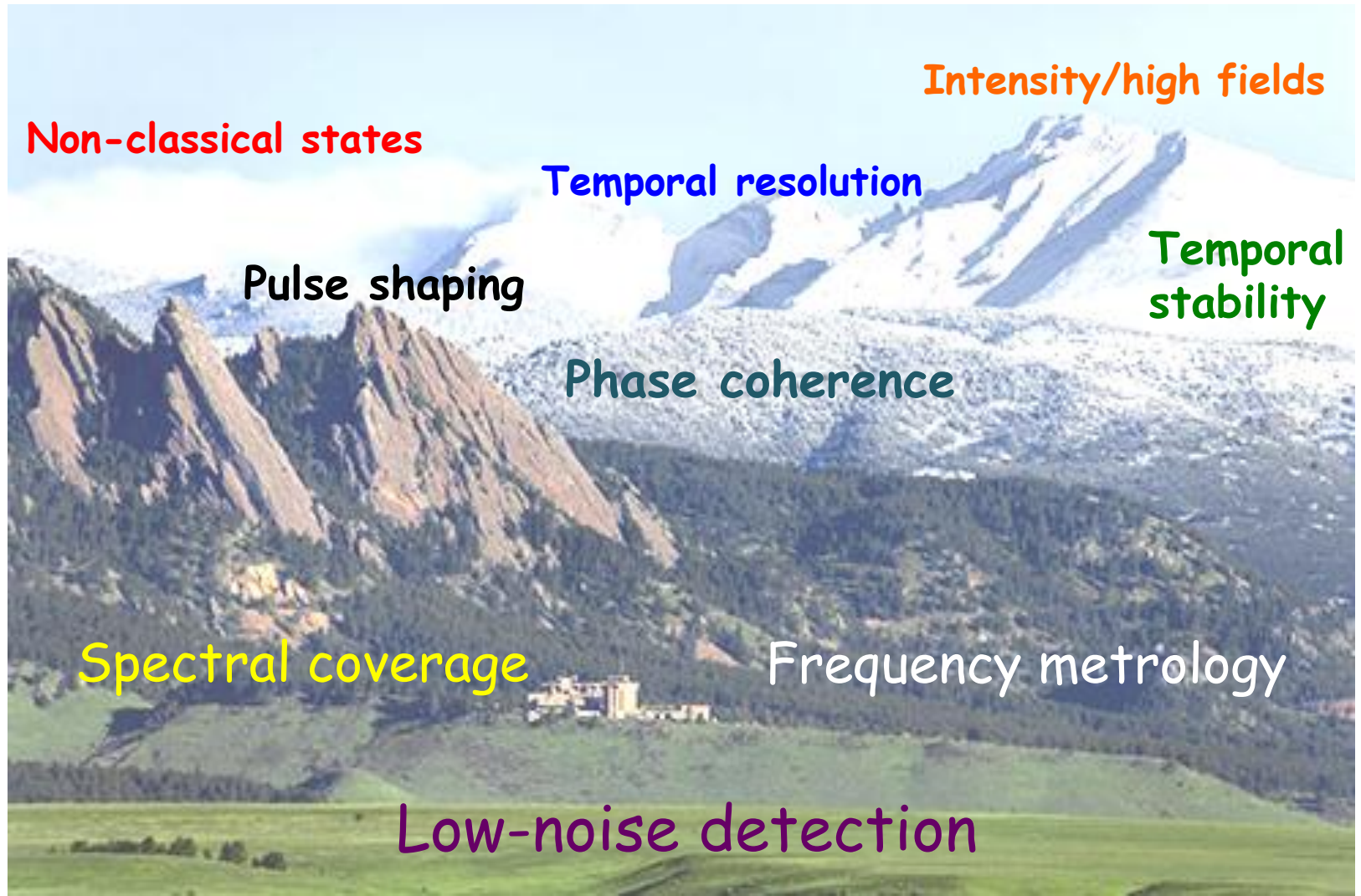
- A remarkable convergence of

Ultracold,
Ultrafast,
Ultrastable,
Ultraprecise

Light at JILA

What makes a versatile photon laboratory?

Scientifically useful photons span a space of many dimensions



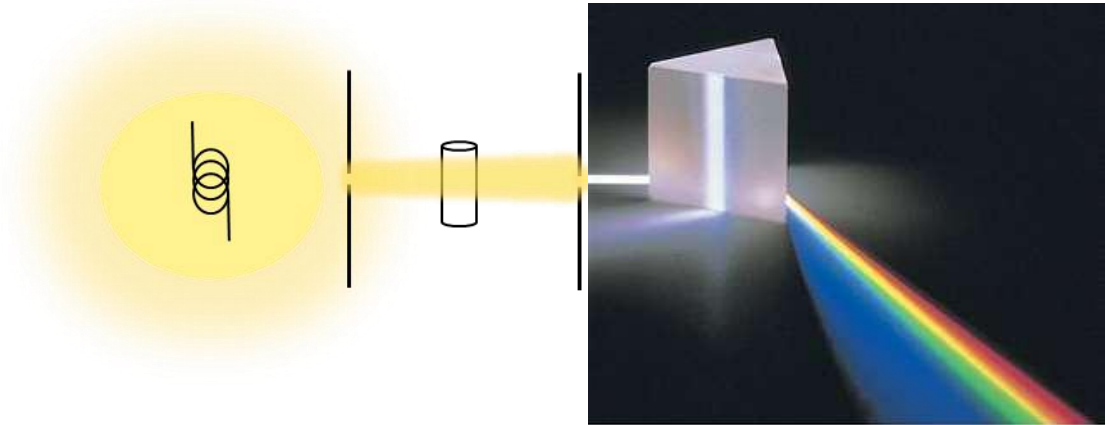
Spectral resolution - Nature's finger prints

Dispersive Spectrometer

- Measure wavelength
- Resolution 10^{-6}

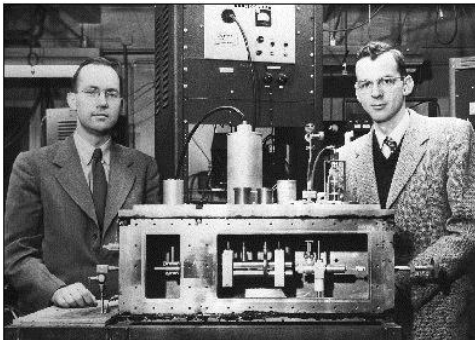


ca. 1660
I. Newton

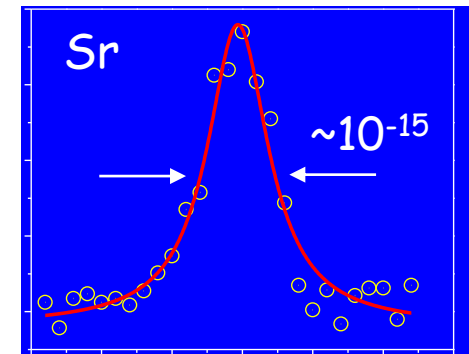
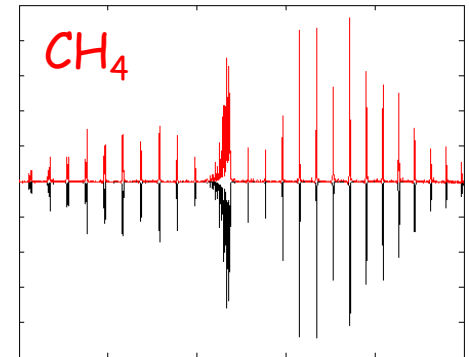
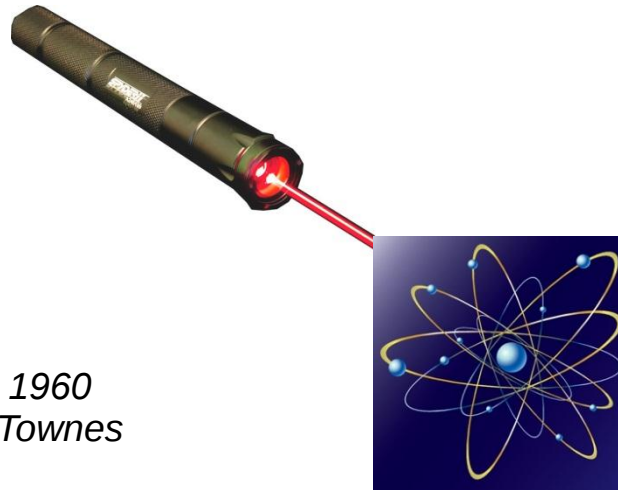


Laser spectroscopy

- Measure frequency
- Resolution 10^{-15}

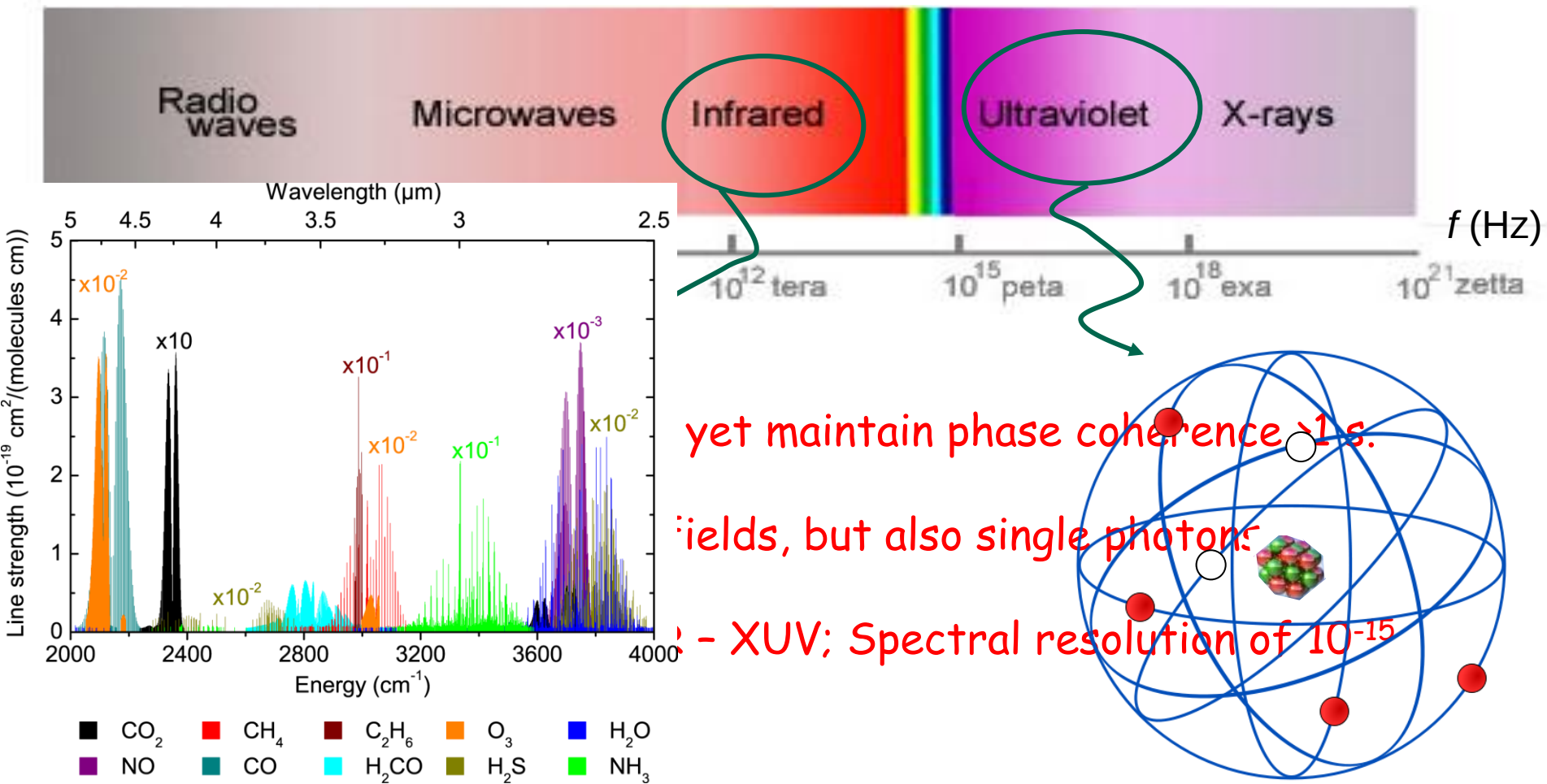


ca. 1960
C. Townes

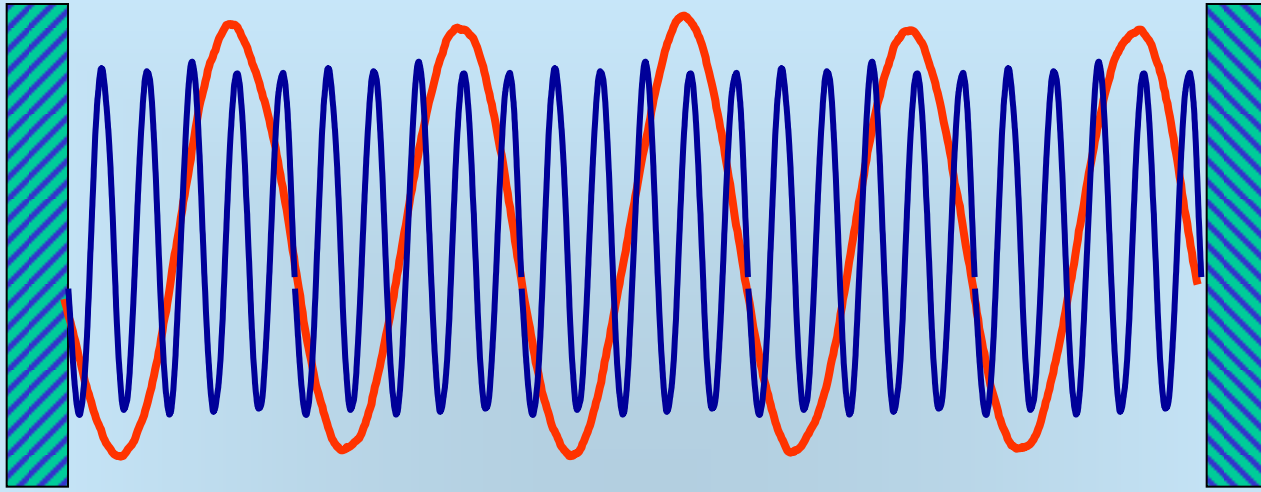


Coherent synthesis of Electromagnetic spectrum

- Phase-coherent radiations - IR to XUV
- Spectroscopy & Quantum Control



Why light ? - Chasing the SPEED!



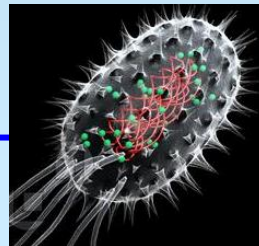
Faster oscillations → More cycles → Smaller errors

Light ripples: 10^{15} cycles per second, & we count every one

Precision: 1 000 000 000 000 000 ± 1

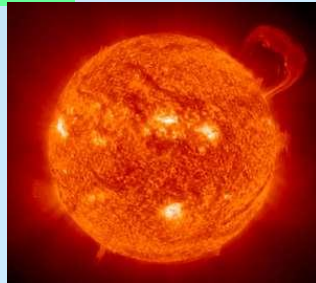


Earth

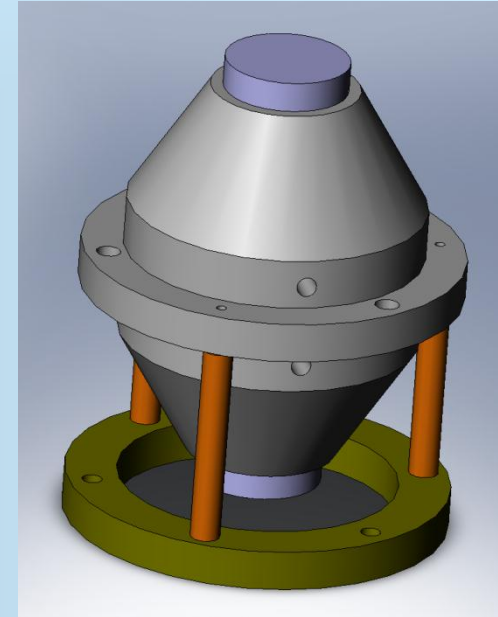


bacteria

Sun

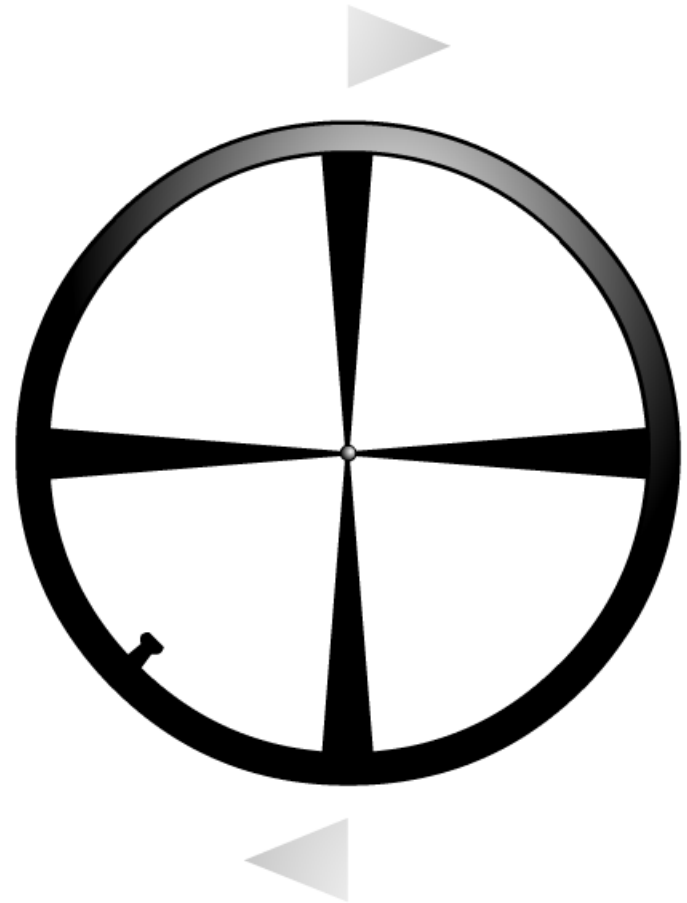
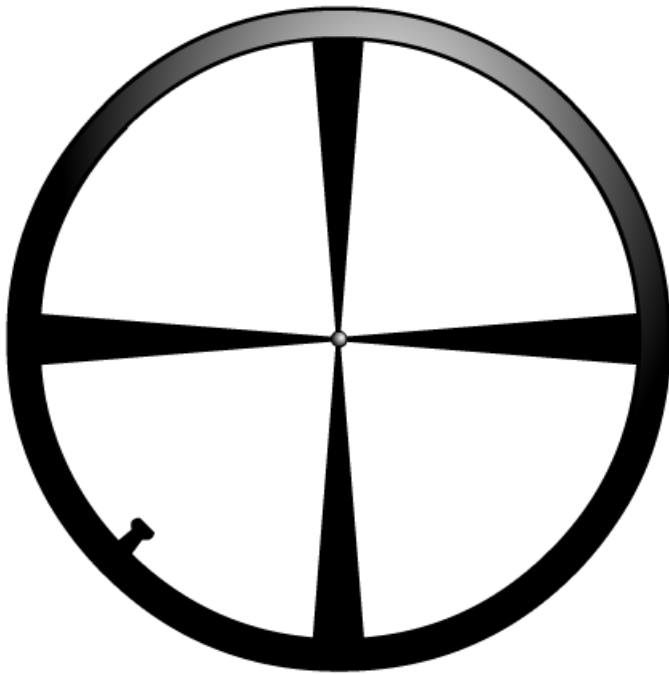


First, make the field steady - Stable optical cavity

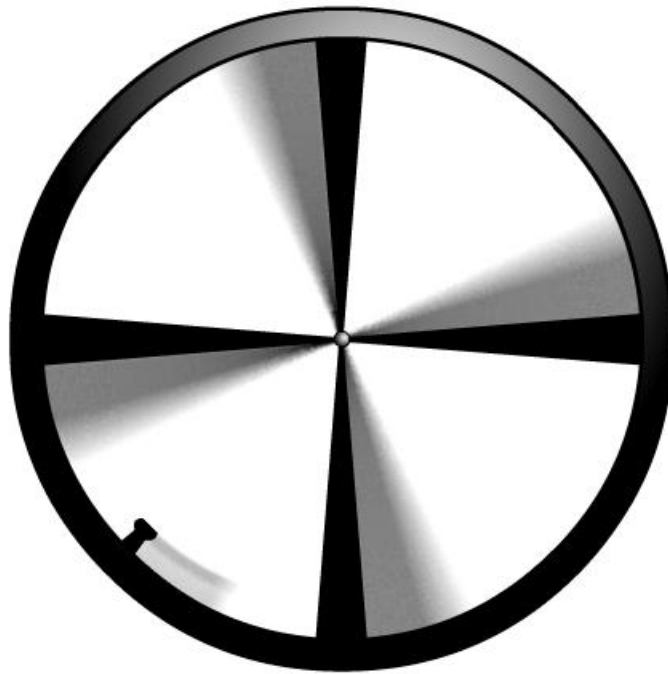


Cavity length 1 m :	fits 10^6 optical waves	(10^{-6})
Finesse 10^5 :	error amplified by 10^5	(10^{-11})
Division of a cycle :	10^5	(10^{-16})

But wait, how do you count so fast?

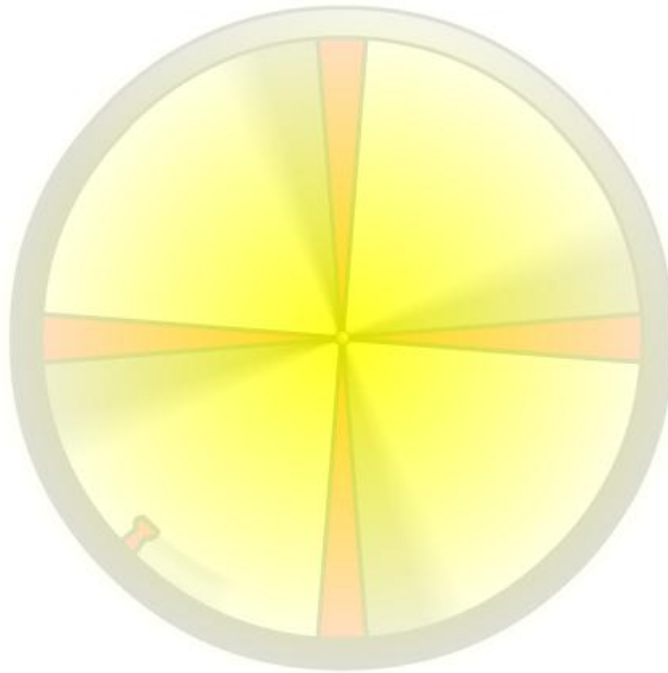


But wait, how do you count so fast?



But wait, how do you count so fast?

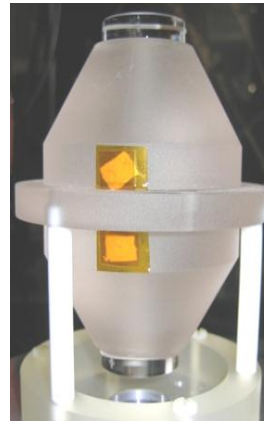
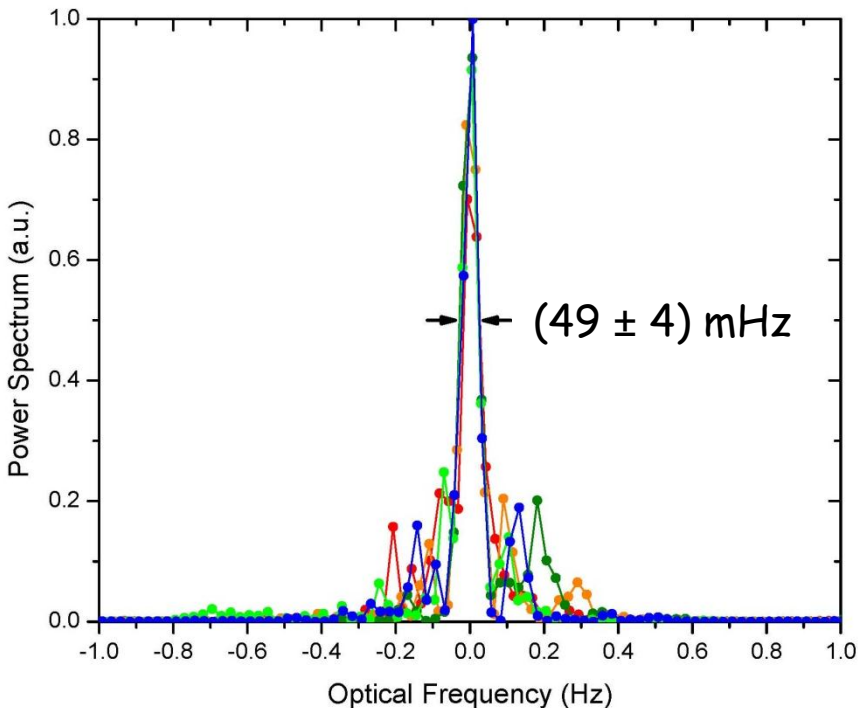
Something runs equally as fast, and very stable!



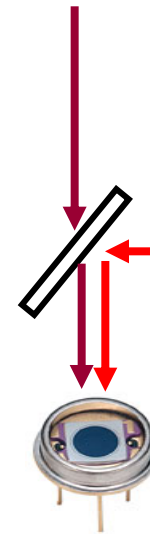
Coherence - how long a wave lasts

~ 10 s

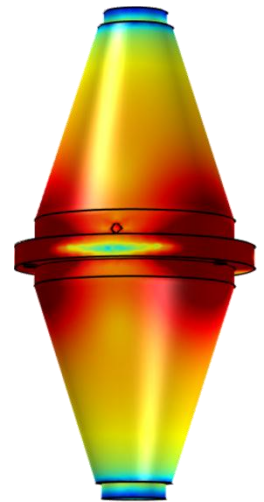
Beating of two optical waves (10^{15} Hz)



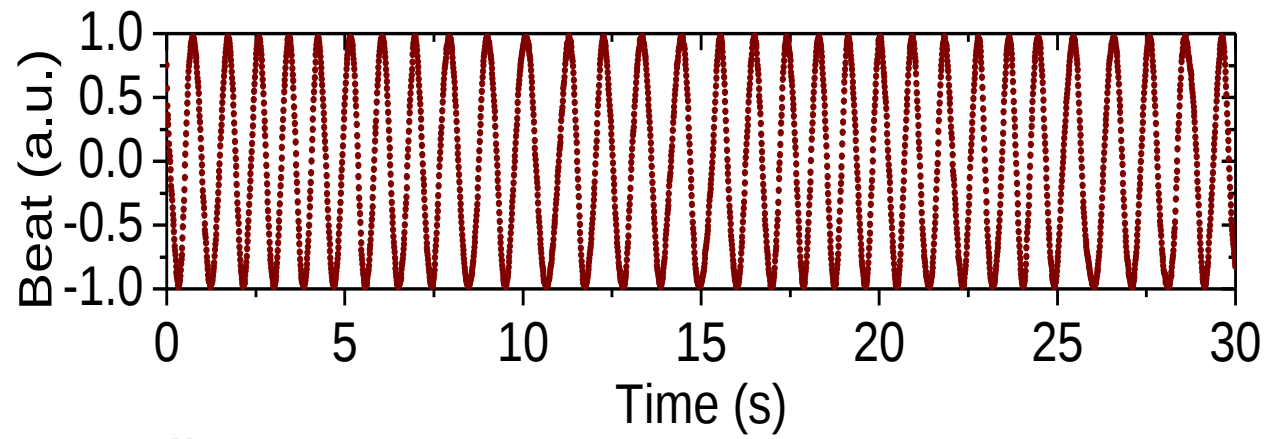
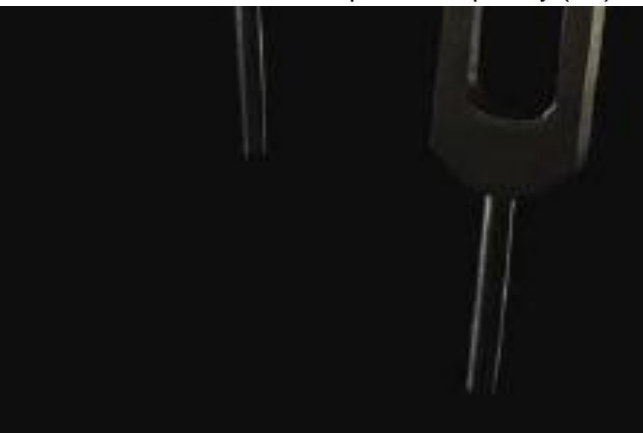
Laser 1



Laser 2

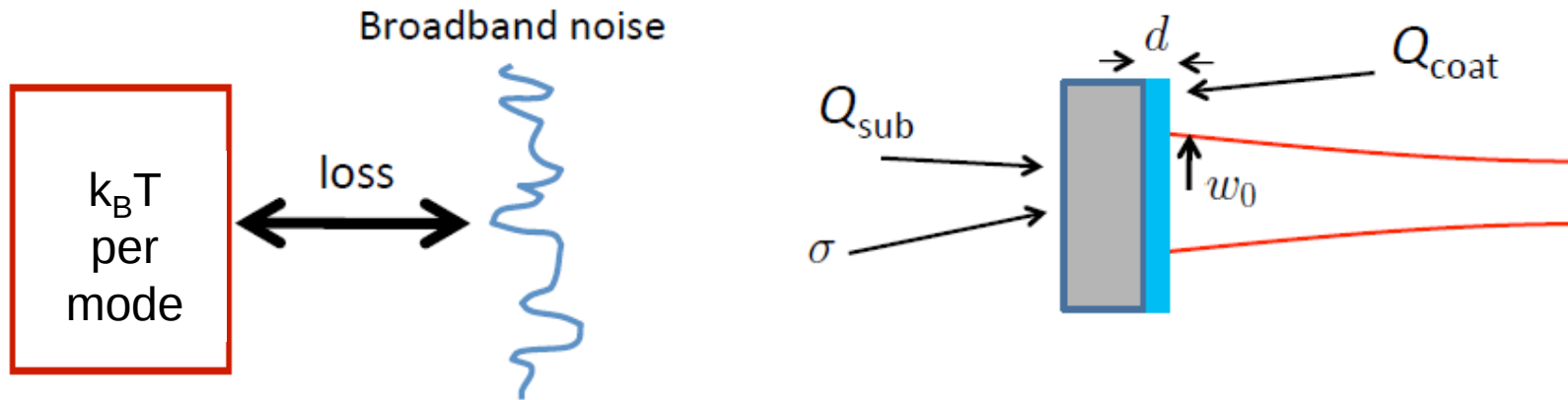


Counting the light ripple (10^{15} Hz)



Mirror thermal noise

Complex (lossy) Young's modulus: $E(\omega) = E_0 [1 + i\phi(\omega)]$



$$S_{x, mirror} \simeq \frac{4k_B T}{\omega} \frac{1 - \sigma^2}{\sqrt{\pi} E w_0} \phi_{sub} \left(1 + \frac{2}{\sqrt{\pi}} \frac{1 - 2\sigma \phi_{coat}}{1 - \sigma} \frac{d}{\phi_{sub} w_0} \right)$$

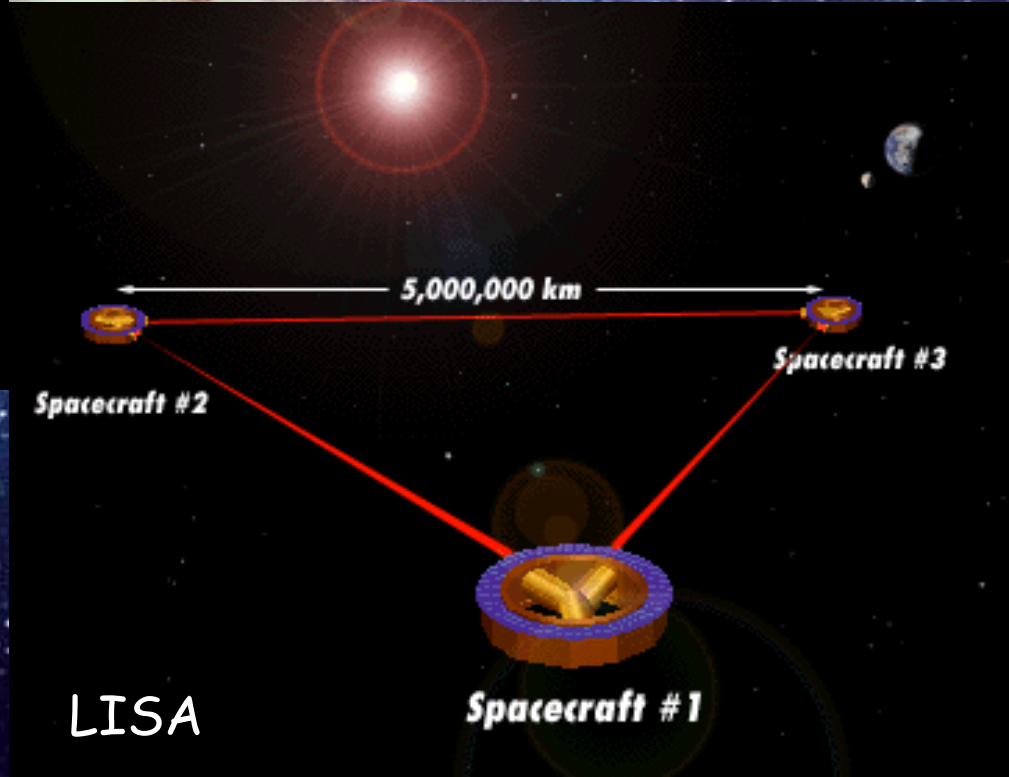
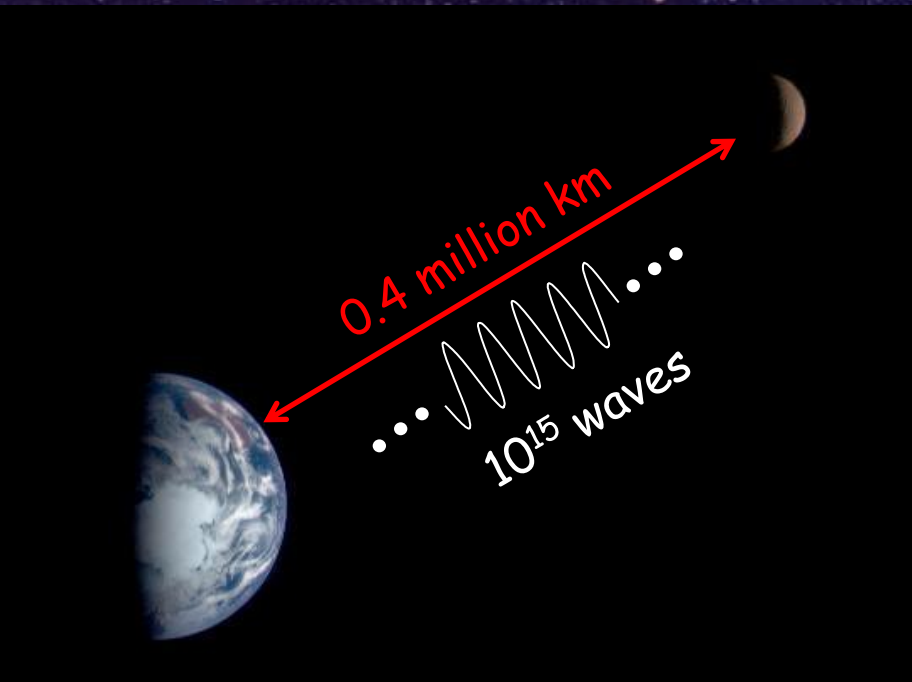
Y. Levin. **PRD** 57, 659 (1997).

K. Numata et. al. **PRL** 93, (2004).

G. M. Harry et. al. **Class. Quant. Grav.** 19, (2002).

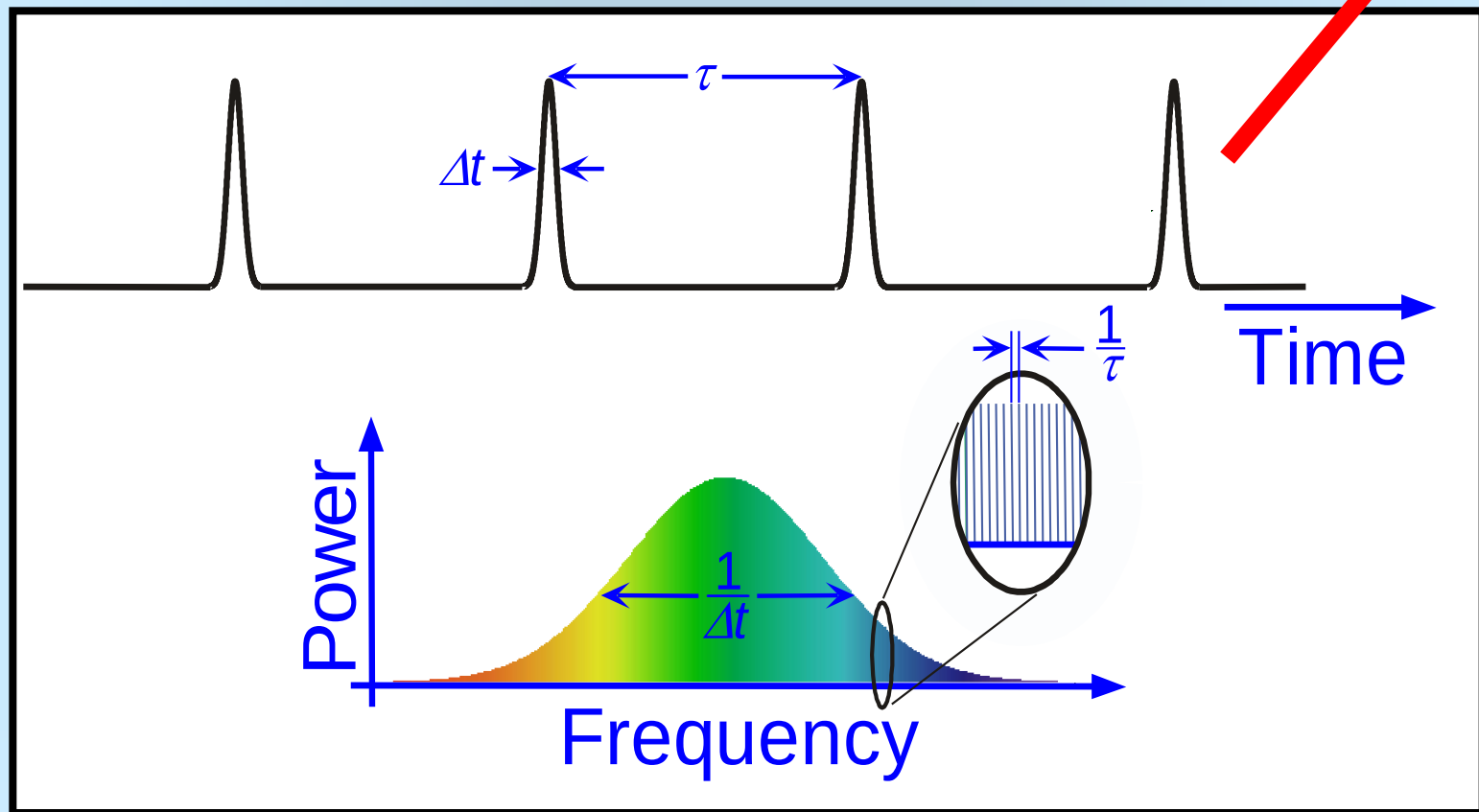
Rulers for the Universe

Testing the fundamental laws of Nature



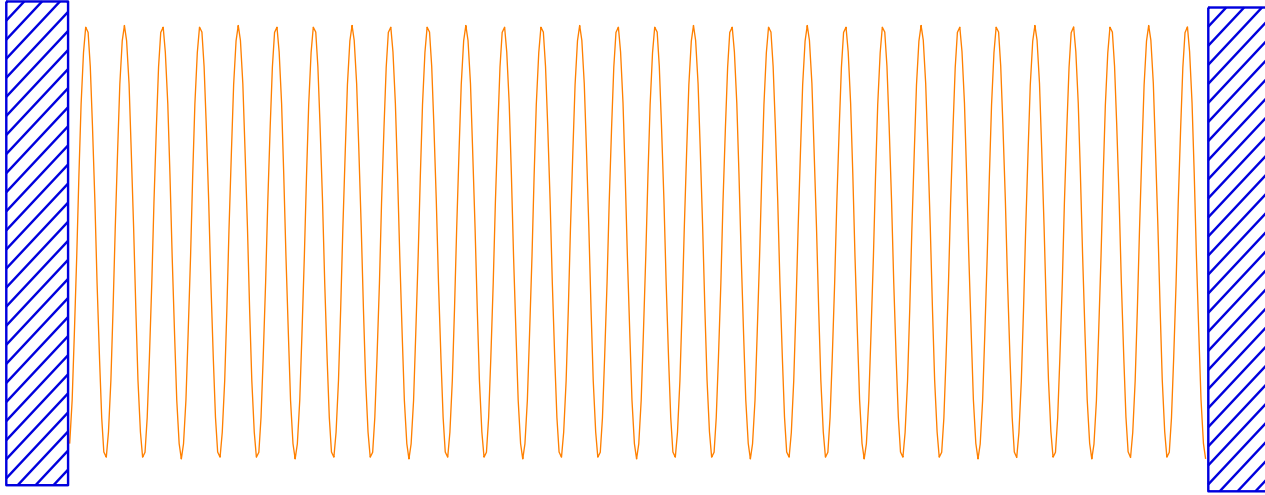
Time - frequency correspondence

- Temporal pulse width $\longleftrightarrow$ Spectrum bandwidth
- Train of pulses $\longleftrightarrow$ comb of frequencies

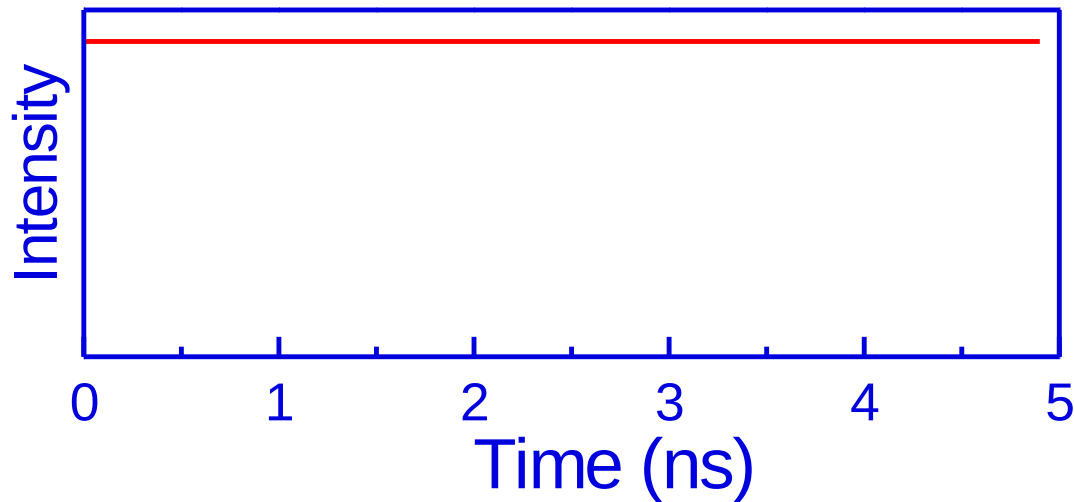


Modelocking

Laser Cavity

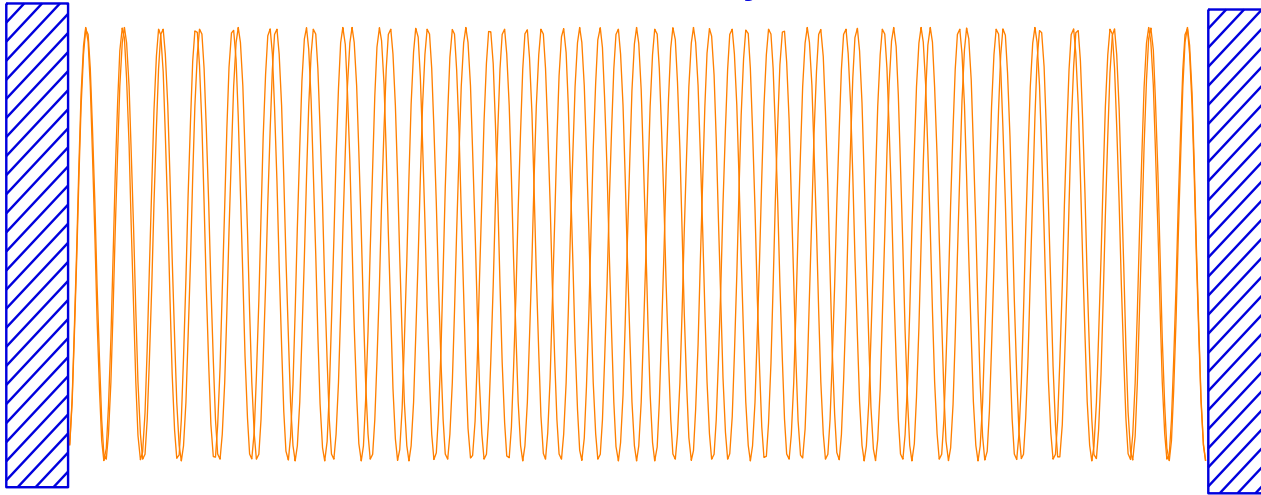


Single mode
cw laser

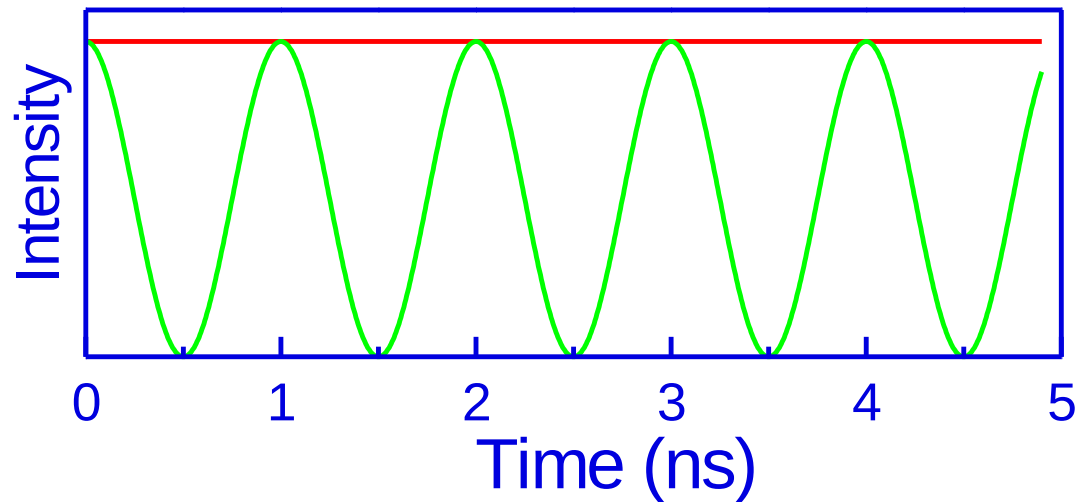


Modelocking

Laser Cavity

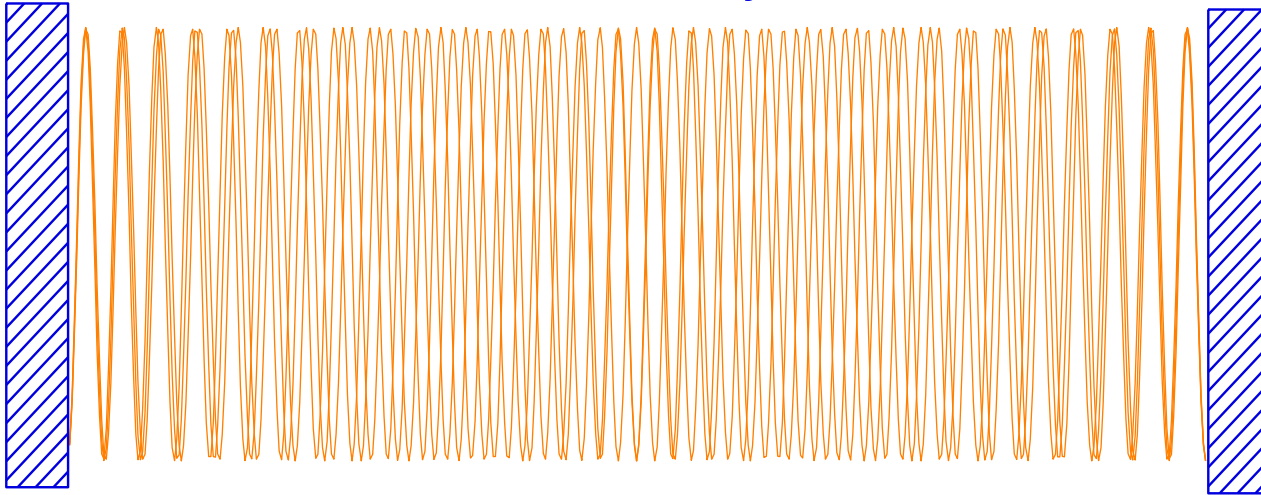


2 modes

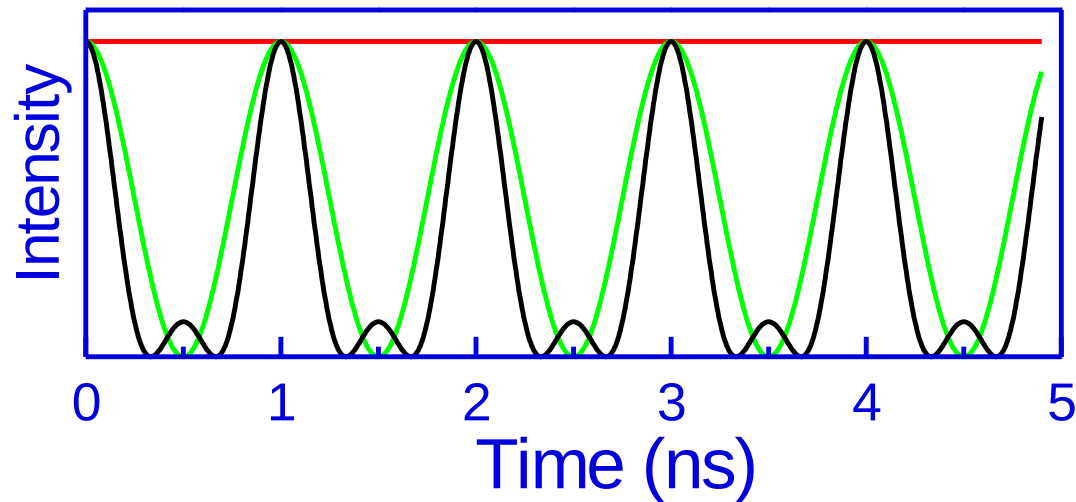


Modelocking

Laser Cavity

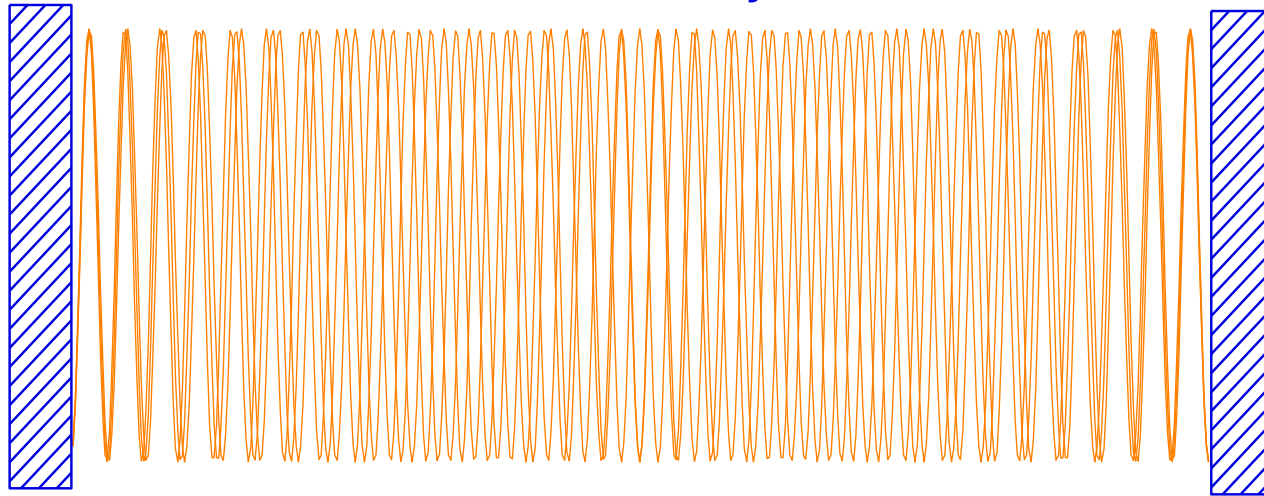


3 modes



Modelocking

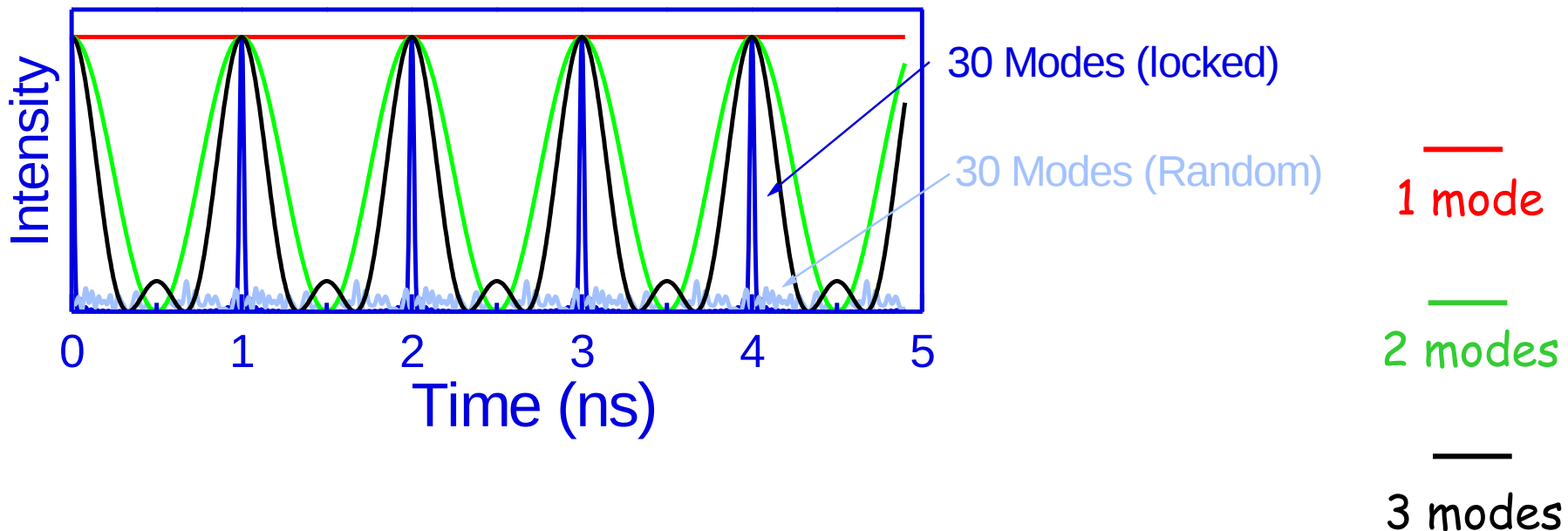
Laser Cavity



2 degrees of freedom:

- single-mode phase
- dispersion

Constructive
interference
among
phase-locked
cavity modes



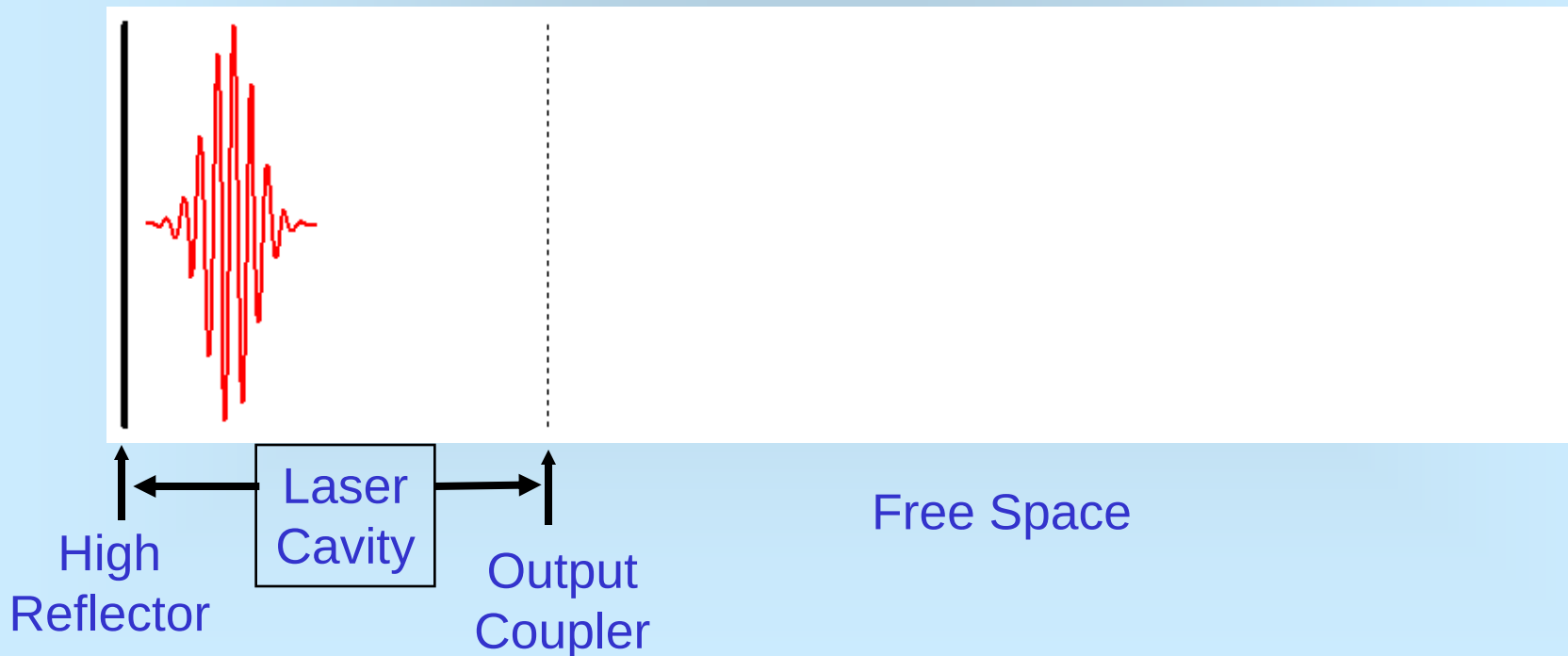
Group vs. Phase Velocity



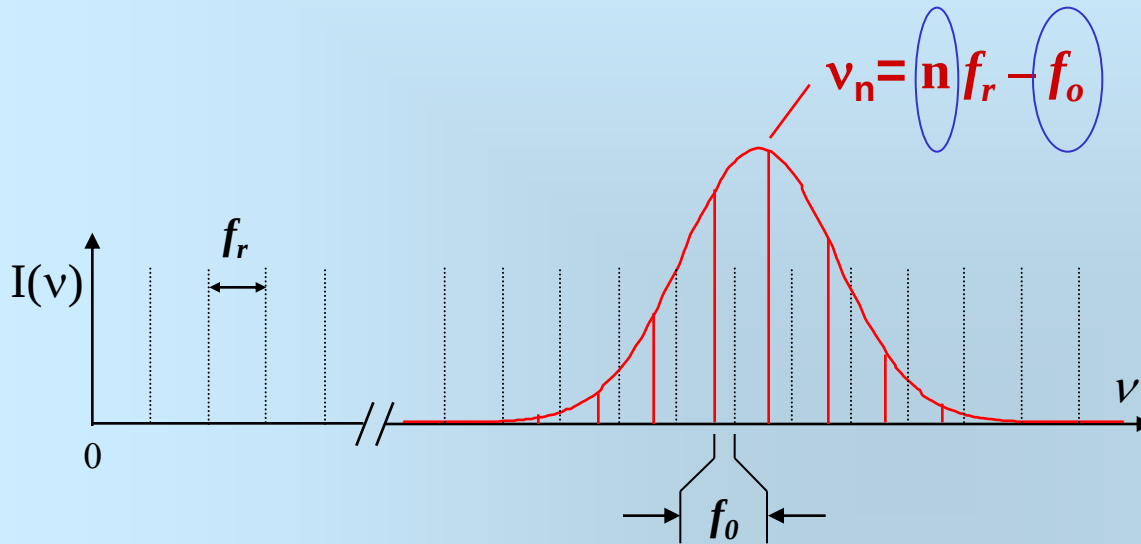
- In any material, the group and phase velocities differ
- Carrier phase slowly drifts through the envelope as a pulse propagates

Group vs. Phase in Modelocked Lasers

Each emitted pulse has a distinct envelope-carrier phase
- due to group-phase velocity difference inside cavity



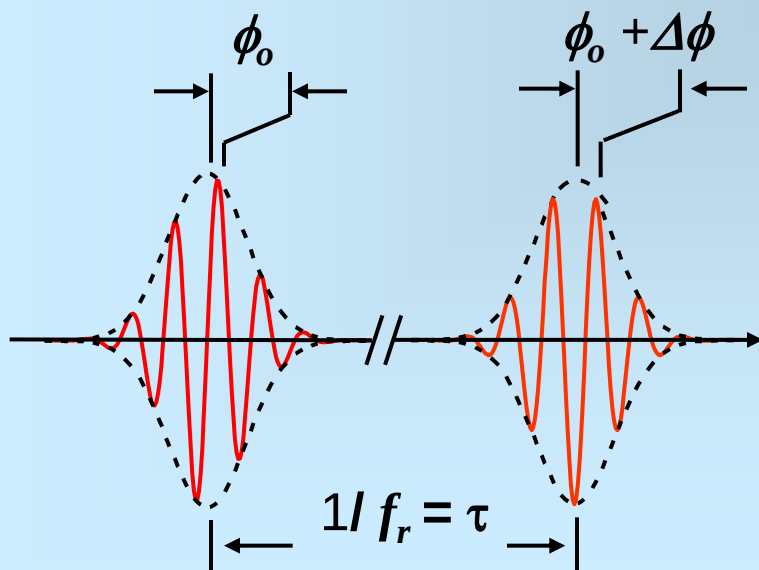
Time- and frequency-domain connections



f_r = Comb spacing

f_o = Comb offset from
harmonics of f_r

$\Delta\phi$ = Phase slip b/t carrier &
envelope each round trip

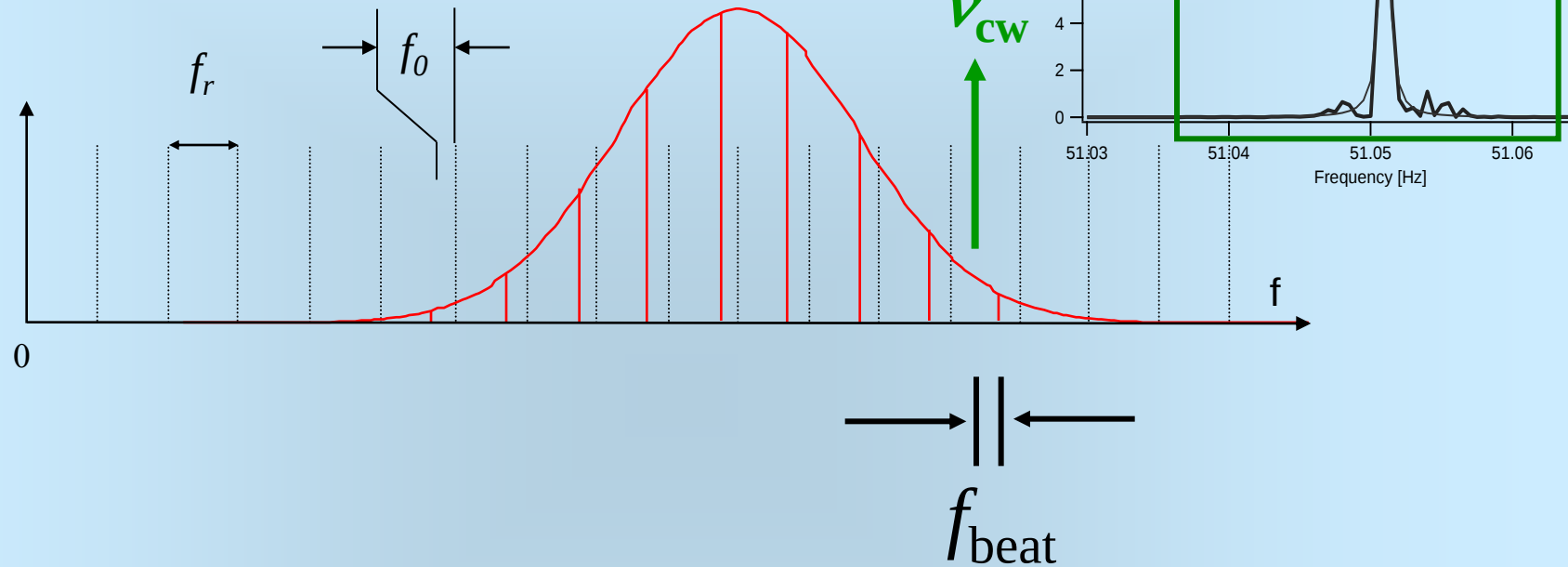


$$2\pi\nu_n \cdot \tau + \Delta\phi = 2n\pi \rightarrow$$

$$\nu_n = n f_r - \underbrace{\Delta\phi f_r / 2\pi}_{f_o}$$

Hänsch, 1978, Garching and Boulder 1999 – 2000
Udem *et al.*, Phys. Rev. Lett. **82**, 3568 (1999).
Diddams *et al.*, Phys. Rev. Lett. **84**, 5102 (2000).

Optical Frequency measurement



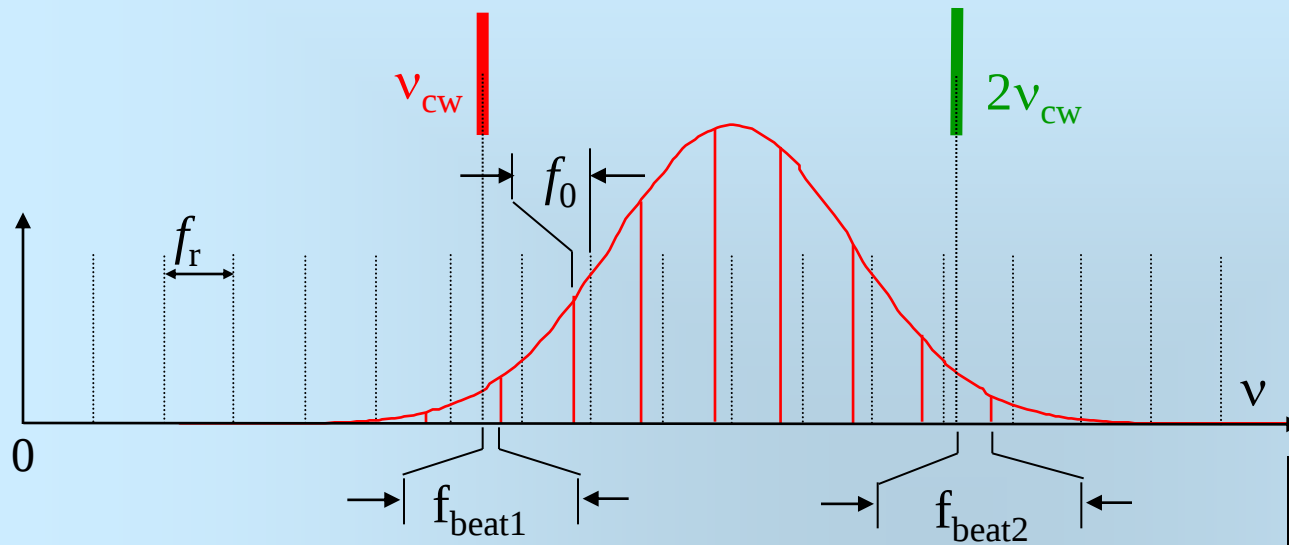
$$f_{beat} = n f_r + f_0 - \nu_{cw}$$

$$f_{beat} + \Delta f_{beat} = n(f_r + \Delta f_r) + f_0 - \nu_{cw}$$

$$n = \Delta f_{beat} / \Delta f_r$$

Optical octave bandwidth

- a quick way to measure and control f_0



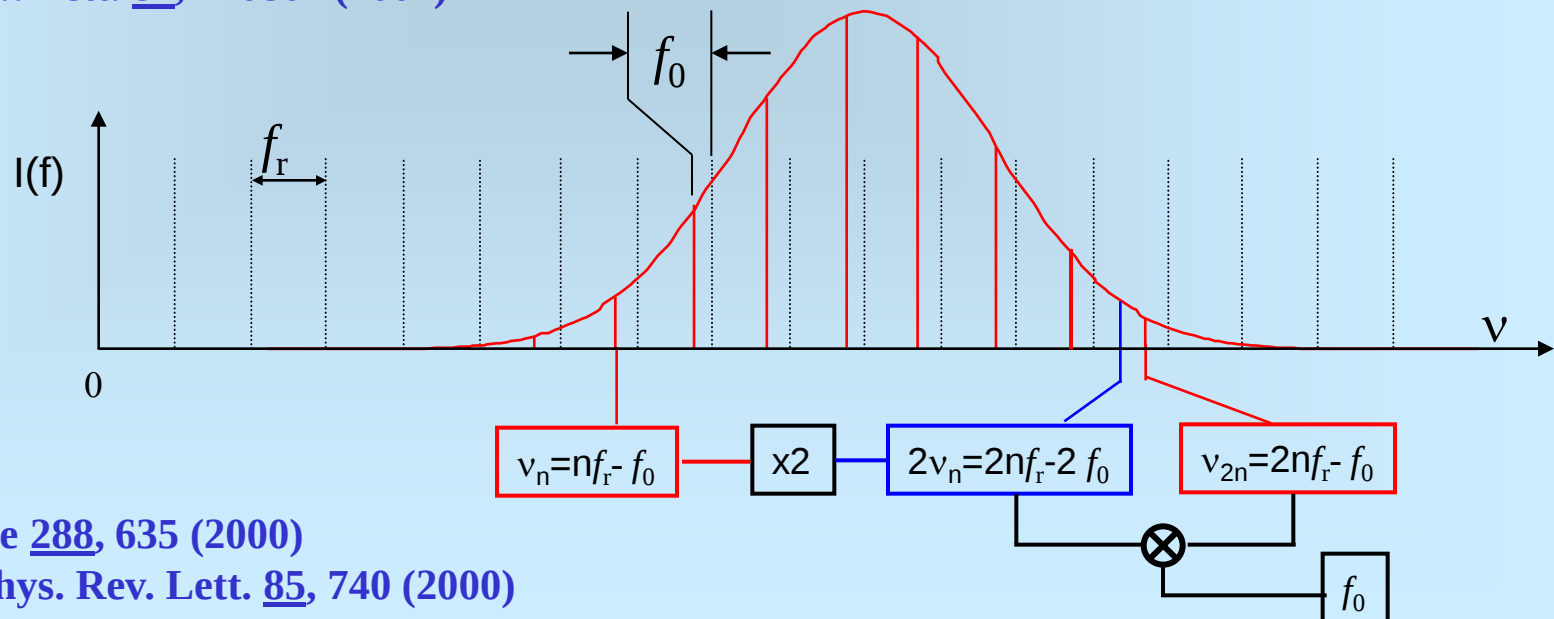
$$f_{beat1} = n f_r + f_0 - \nu_{cw}$$

$$f_{beat2} = 2n f_r + f_0 - 2\nu_{cw}$$

$$f_0 = 2f_{beat1} - f_{beat2}$$

$$f_r = (\nu_{cw} - f_{beat1} - f_0)/n$$

Ye *et al.*, Phys. Rev. Lett. 87, 270801 (2001)



Jones *et al.*, Science 288, 635 (2000)

Apolonski *et al.*, Phys. Rev. Lett. 85, 740 (2000)

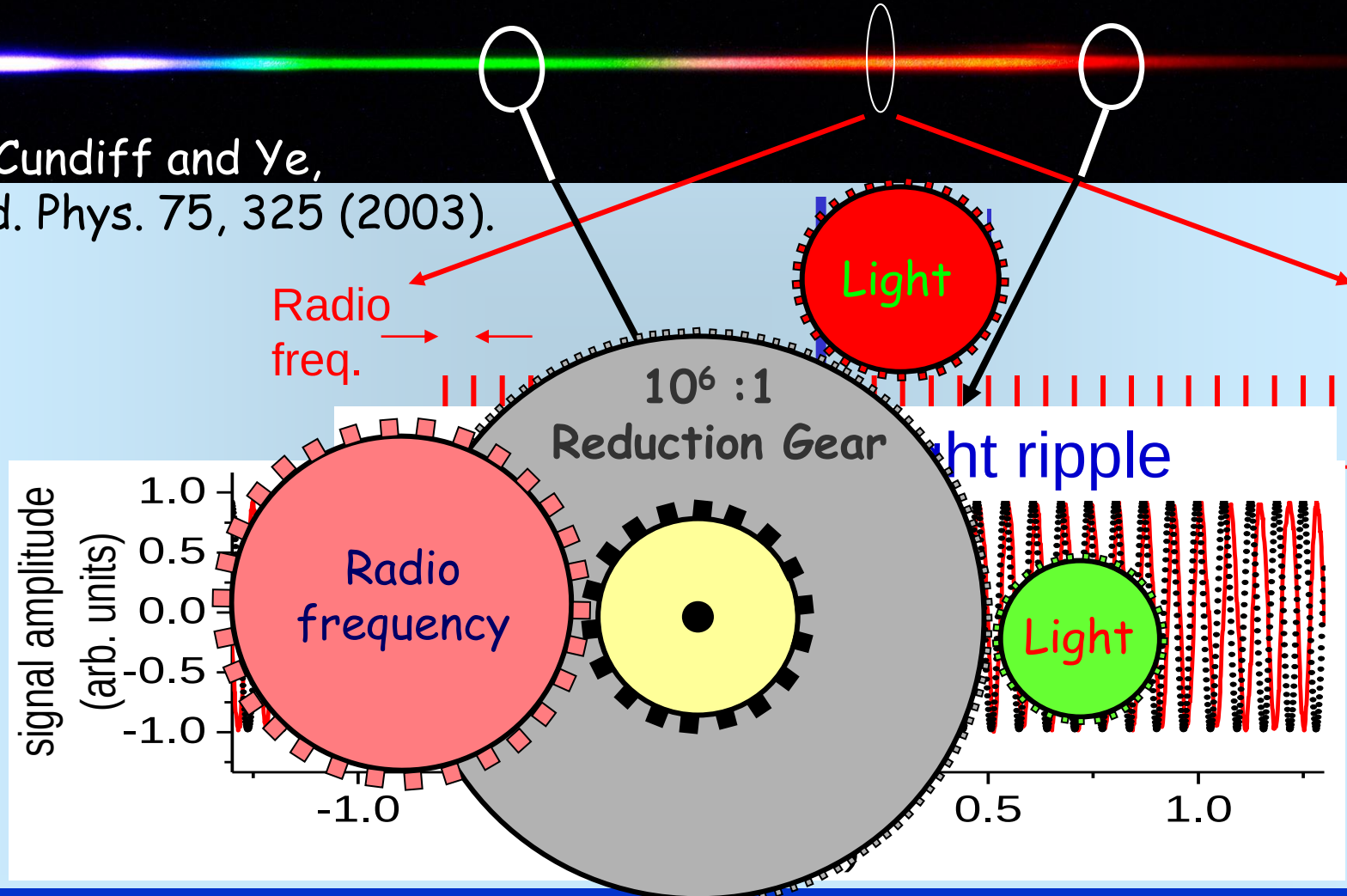
A rainbow spectrum with 10^{-19} precision

Hall and Hänsch, 2005 Nobel Prize

Optical frequency comb

Cundiff and Ye,

Rev. Mod. Phys. 75, 325 (2003).



Optical coherence time > 1 s ($< 10^{-15}$), anywhere in the visible
Schibli *et al.*, Nature Photonics 2, 355 (2008).

Frequency spectrum in optical frequency synthesis

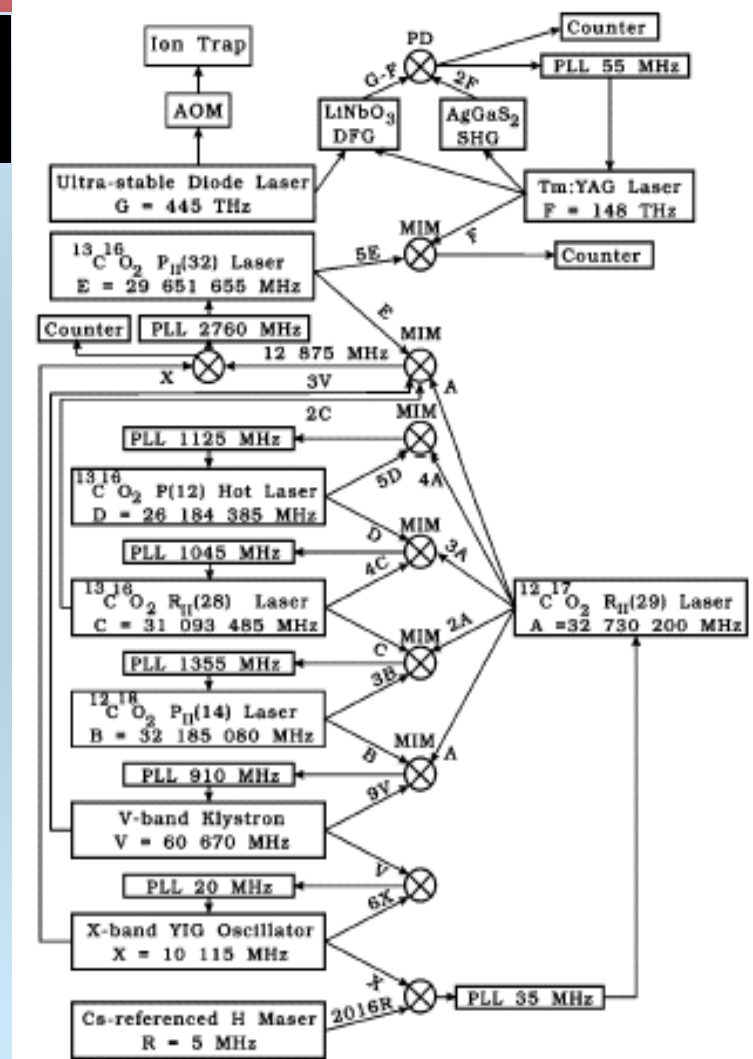
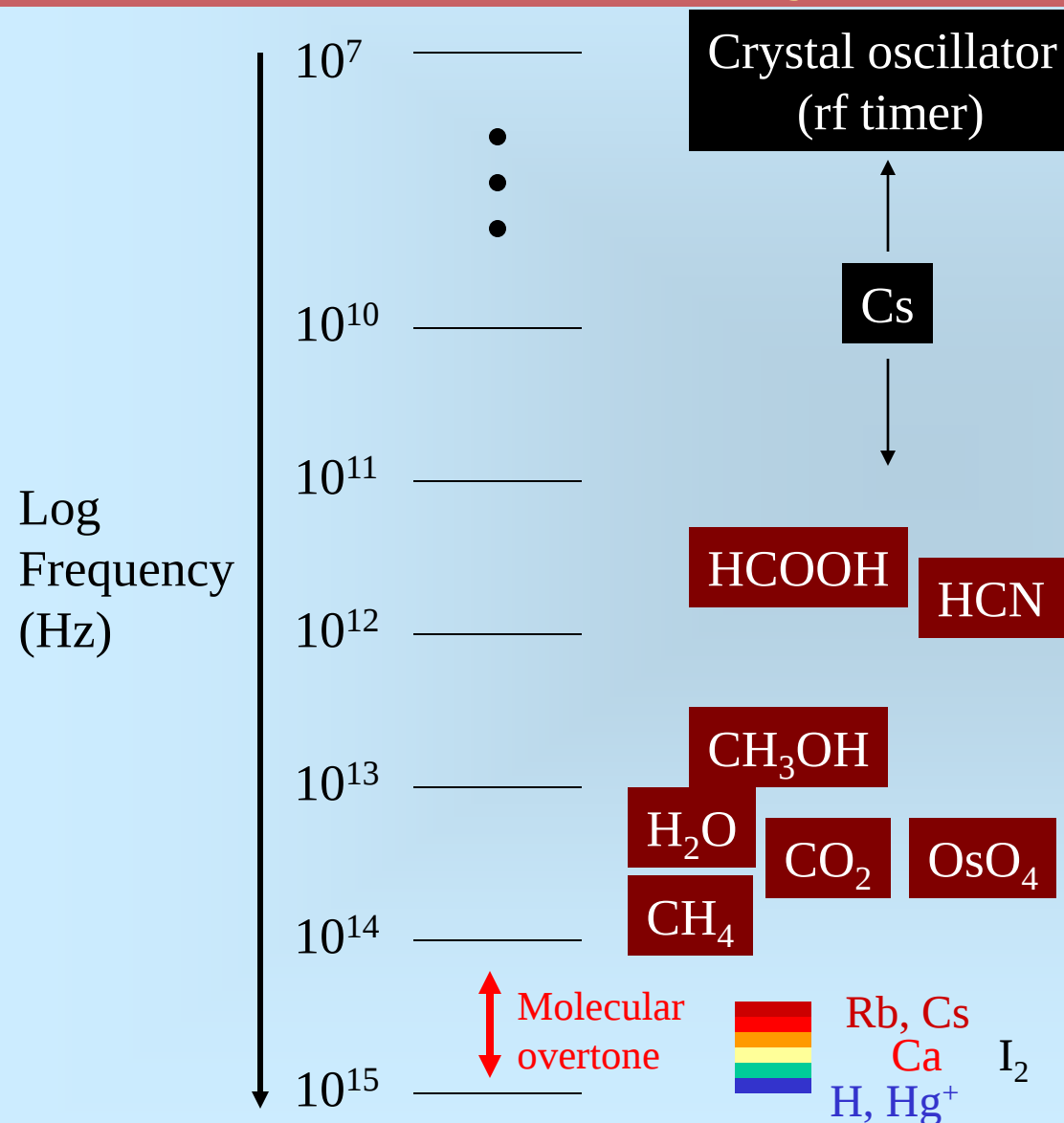
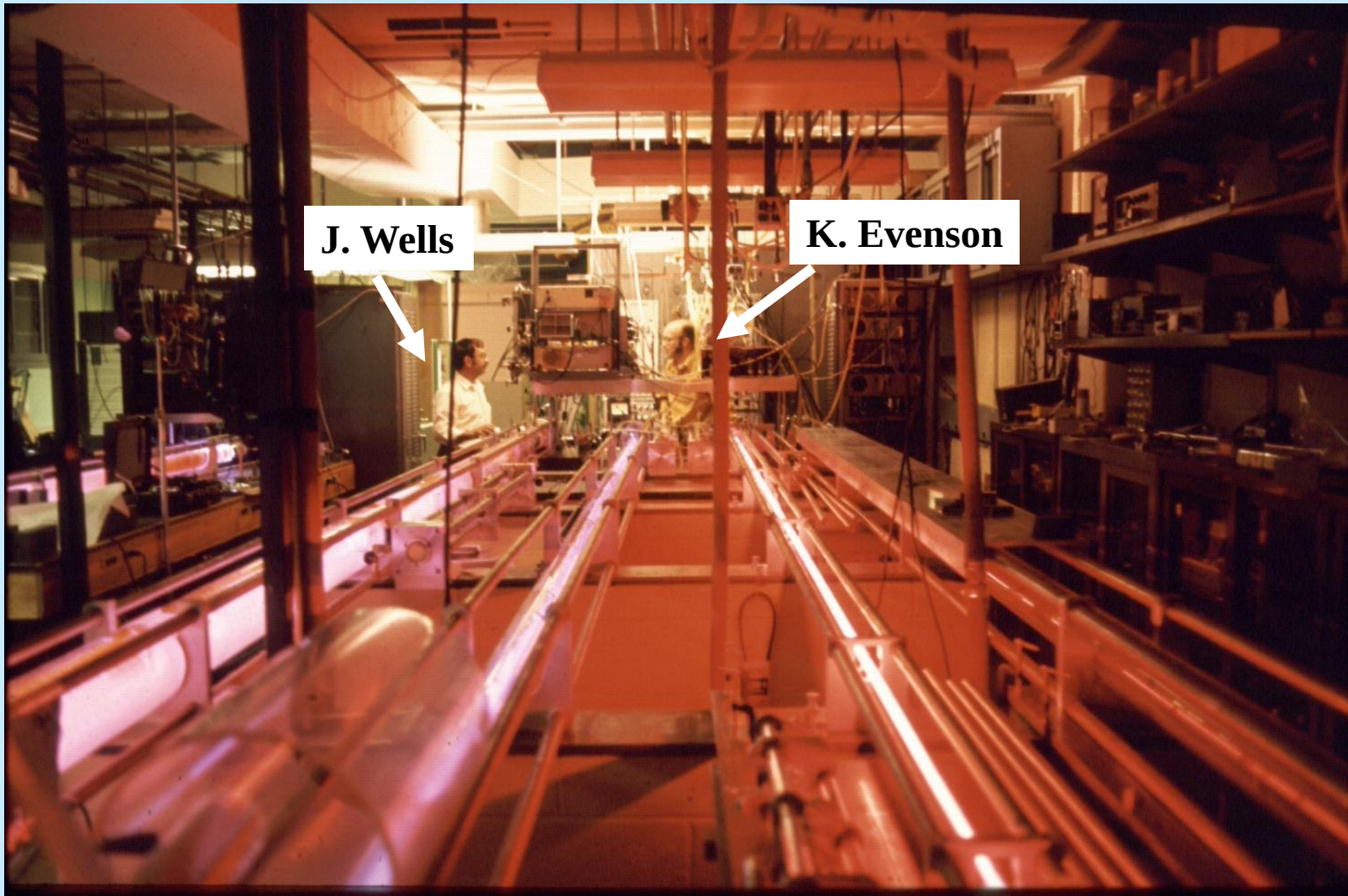


FIG. 1. The frequency chain in the measurement of the optical frequency of the $^{12}\text{C}^{18}\text{O}_2$ laser line. Harmonic frequency chains, PTB, NRC, ...
H. Schnatz *et al.*, PRL 76, 18 (1996).

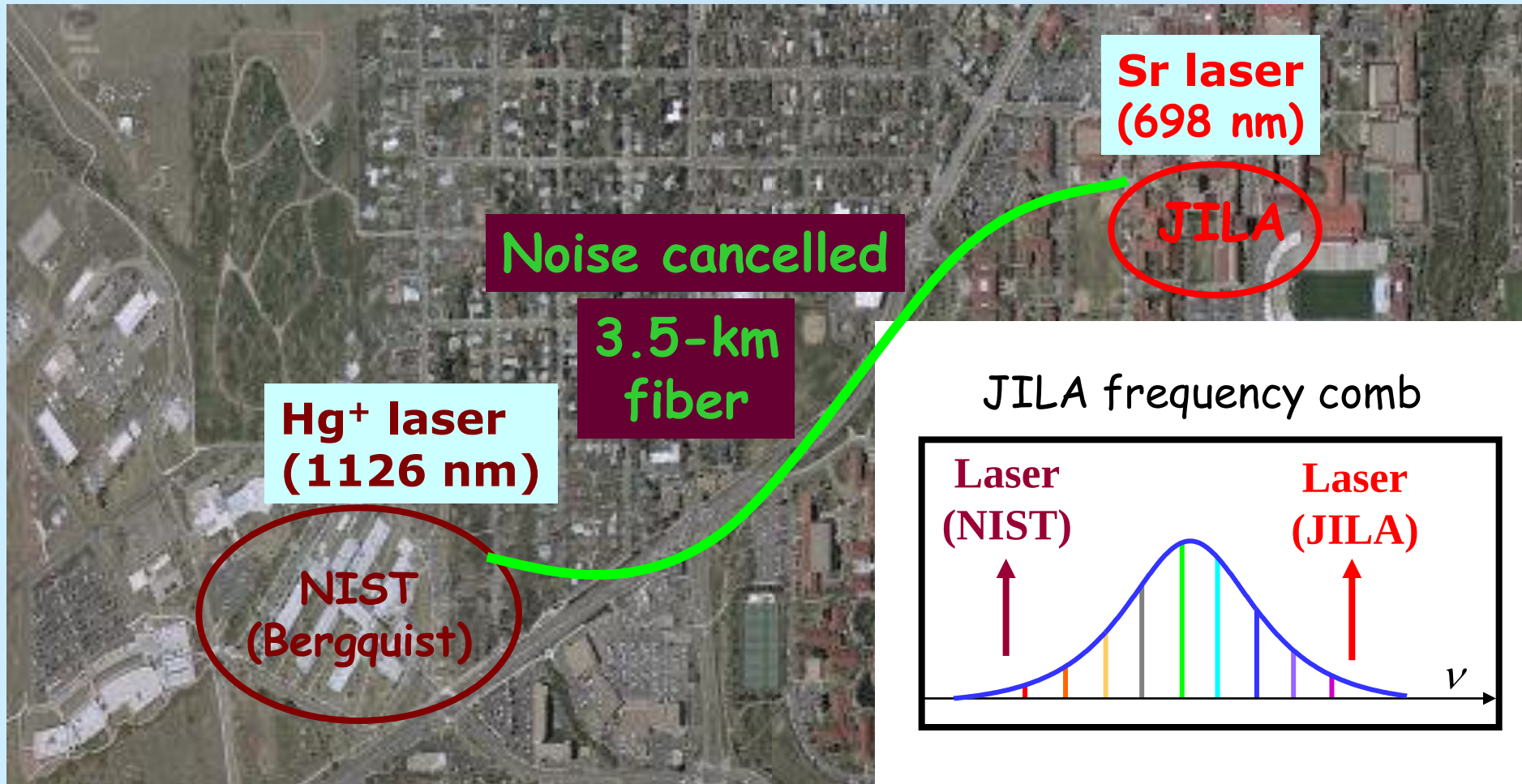
The First Optical Frequency Chain

NBS (NIST): measurement of speed of light, 1972



Optical comparison at 1-Hz

- two spatially & spectrally separated lasers

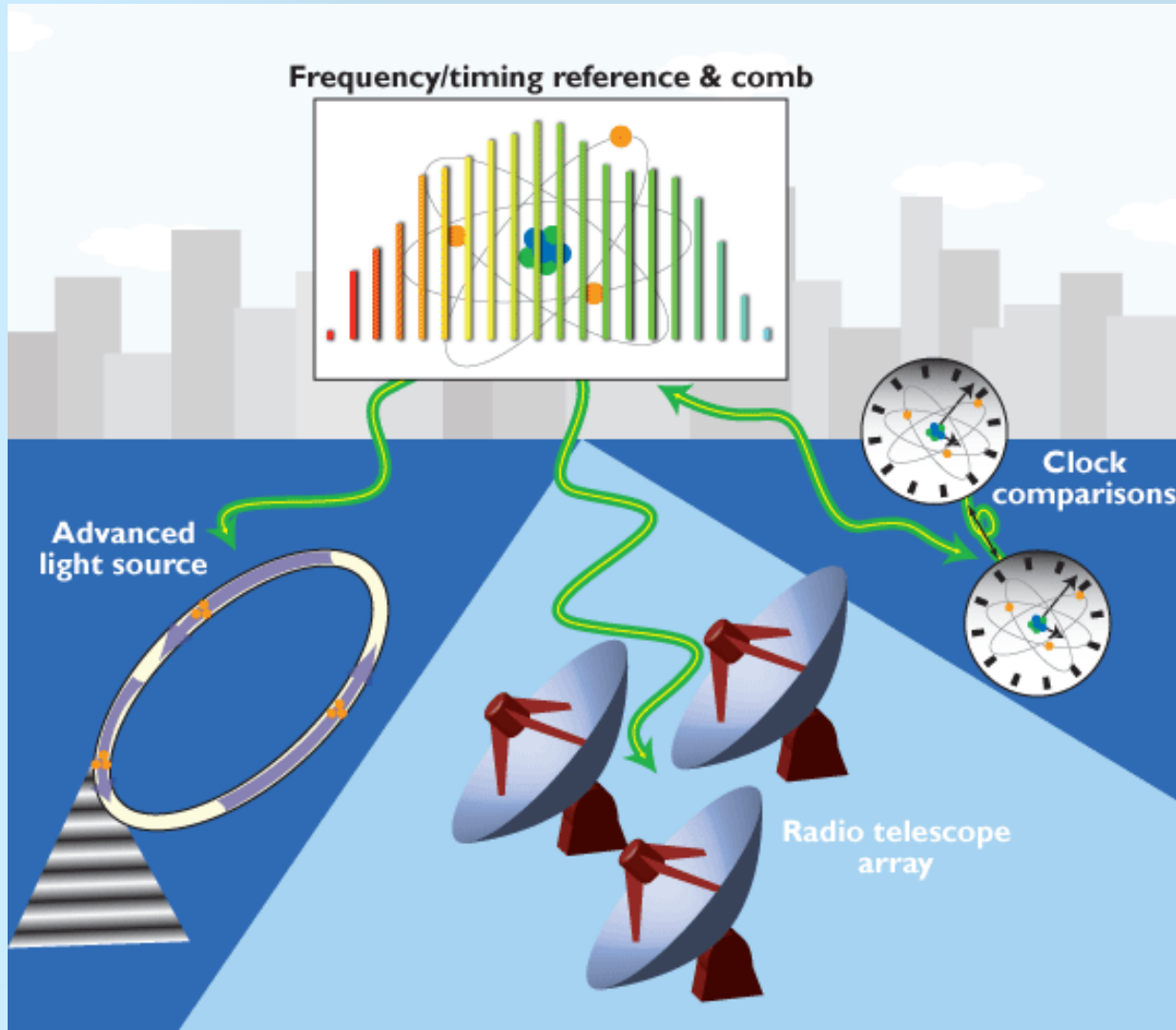


Foreman et al., Phys. Rev. Lett. 99, 153601 (2007).

Precise distribution of ultra-stable signals

Foreman, Holman, Hudson, Jones, and Ye,
Rev. Sci. Instrum. 78, 021101 (2007).

SYRTE, NIST, ...



100 km fiber:

1×10^{-17} @ 1 s;

1 Hz optical
linewidth;

0.1 fs jitter
(20 MHz BW)

Optical lattice - a many-body quantum system

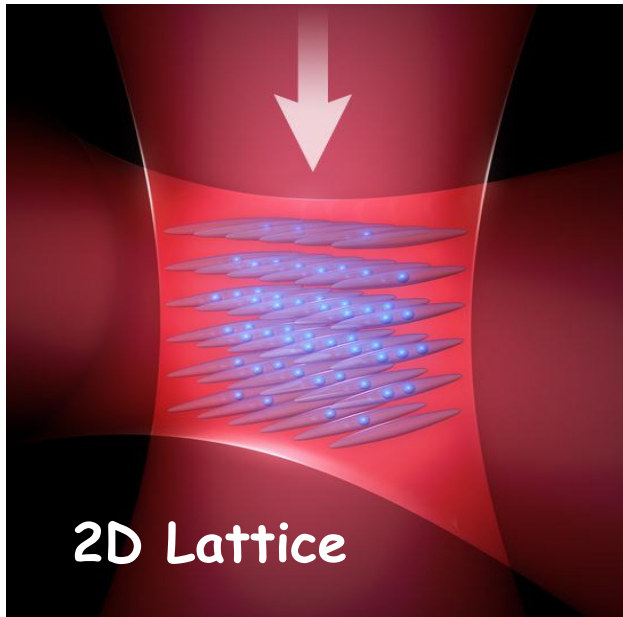
Science **331**, 1043 (2011)

- ✓ Engineered quantum states → eliminating motional effects
- ✓ Separation of internal and external degrees of freedom
- ✓ Isolation from environment
- ✓ Long coherence times
- ✓ Large atom numbers to increase signal and accuracy

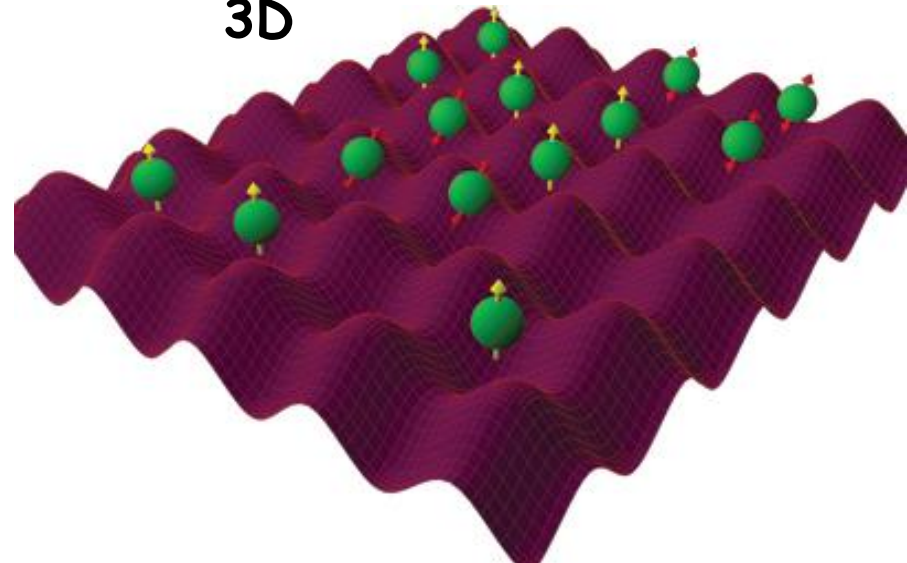
1D Lattice



2D Lattice



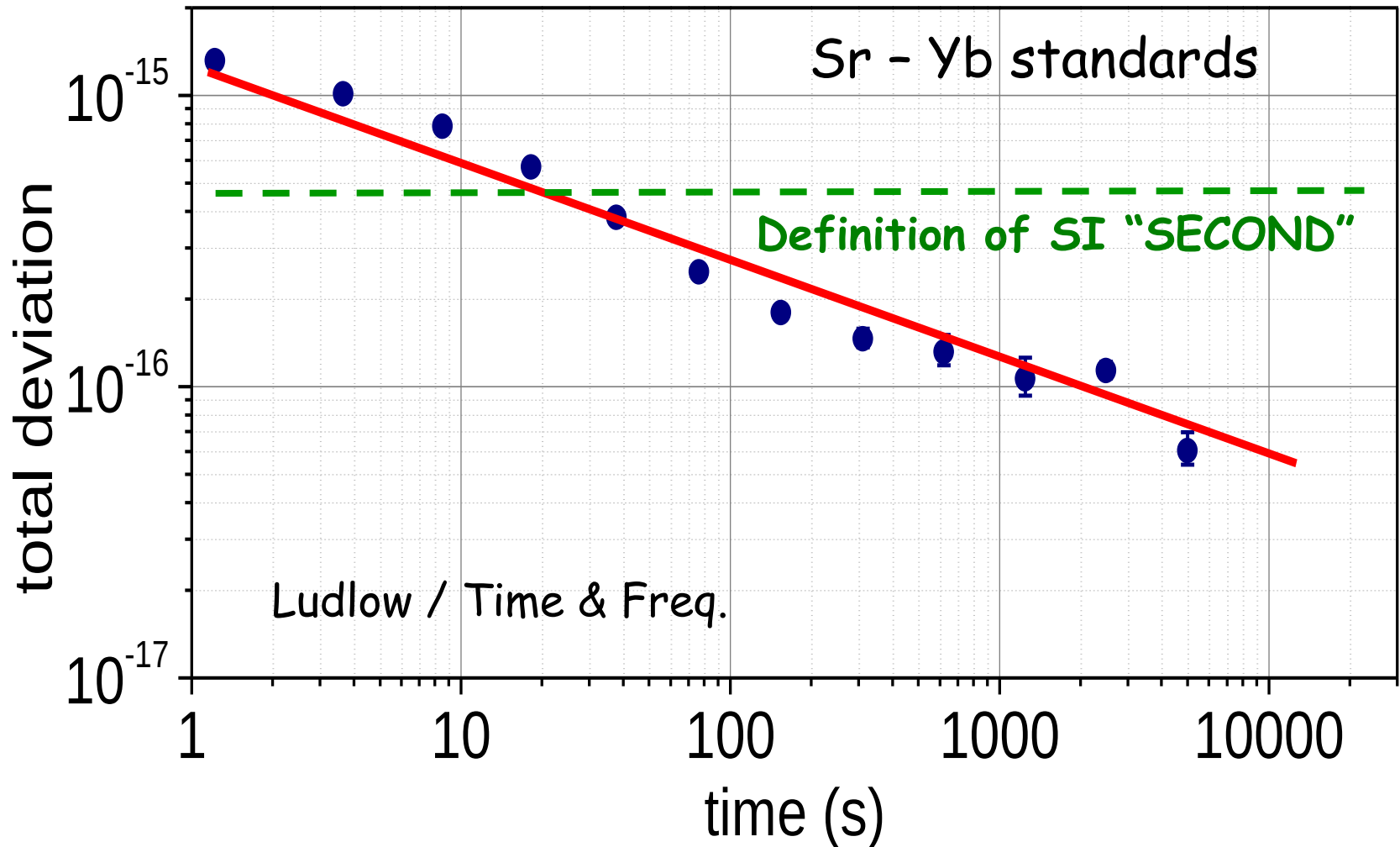
3D



JILA Sr atomic clock

Science **314**, 1430 (2006); Science **319**, 1805 (2008); Science **320**, 1734 (2008); Science **324**, 360 (2009); Science **331**, 1043 (2011).

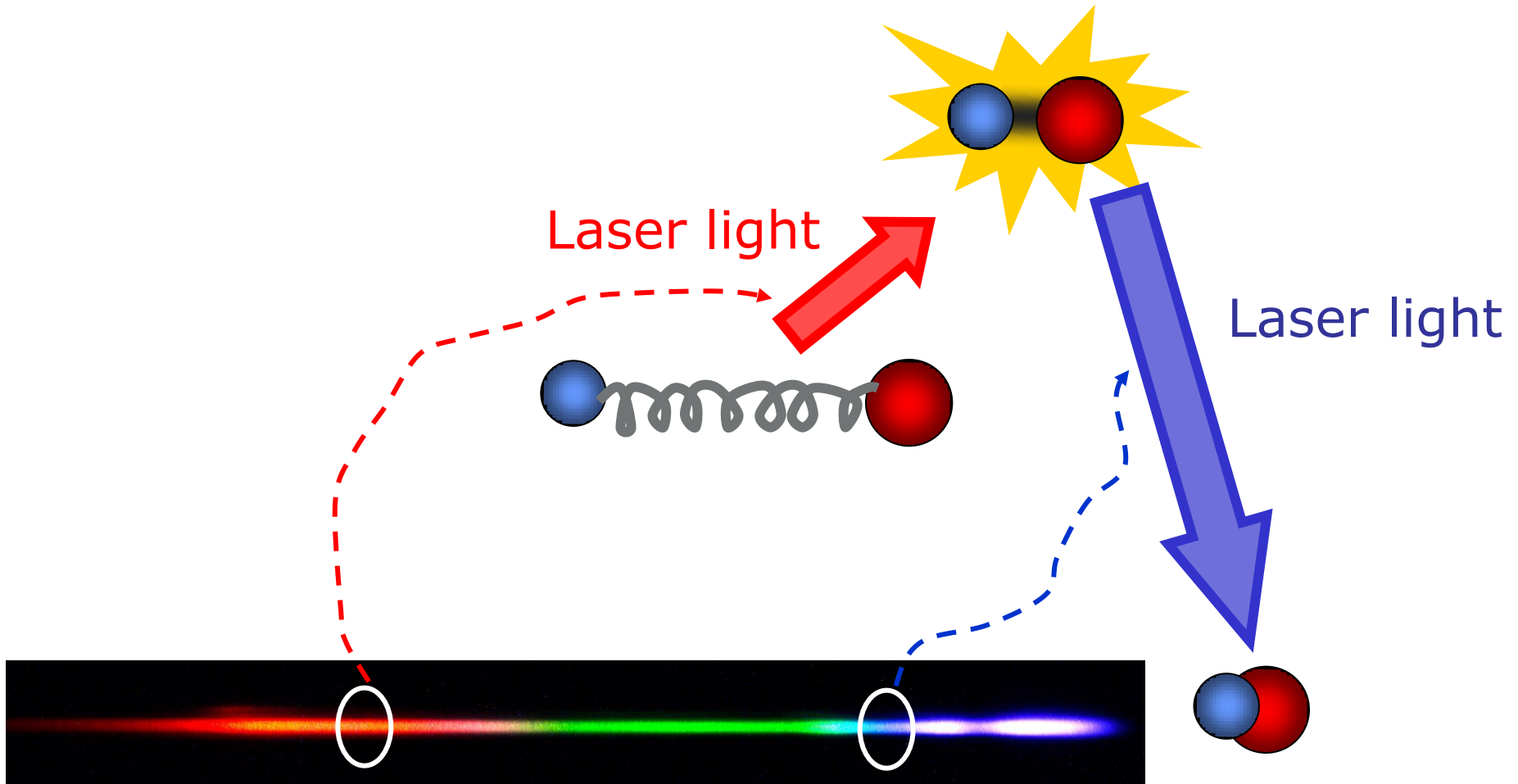
$10,000,000,000,000,000 \pm 1 \quad (10^{-16})$



Teach atoms to make molecules

- chemistry near absolute zero

Photons carry away the energy!



Polar molecules in the quantum regime

D. Jin

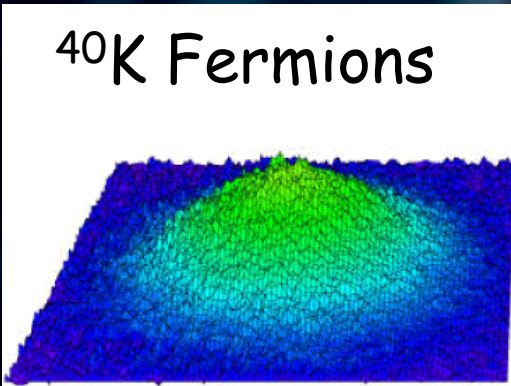
J. Ye

Science 322, 231 (2008)

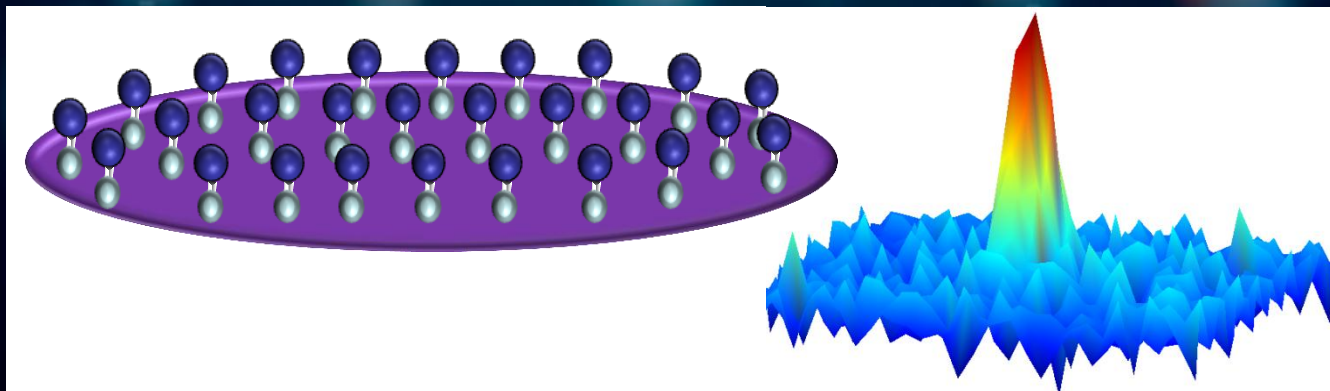
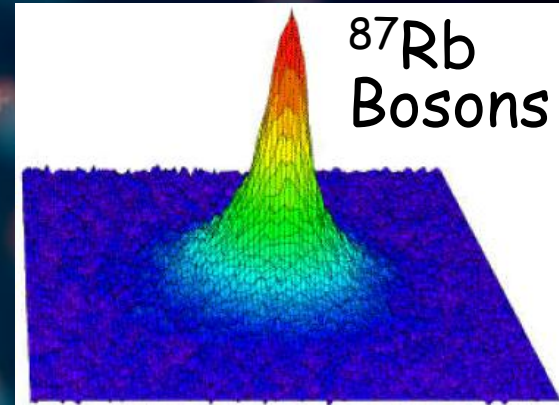
Science 327, 853 (2010)

Nature 464, 1324 (2010)

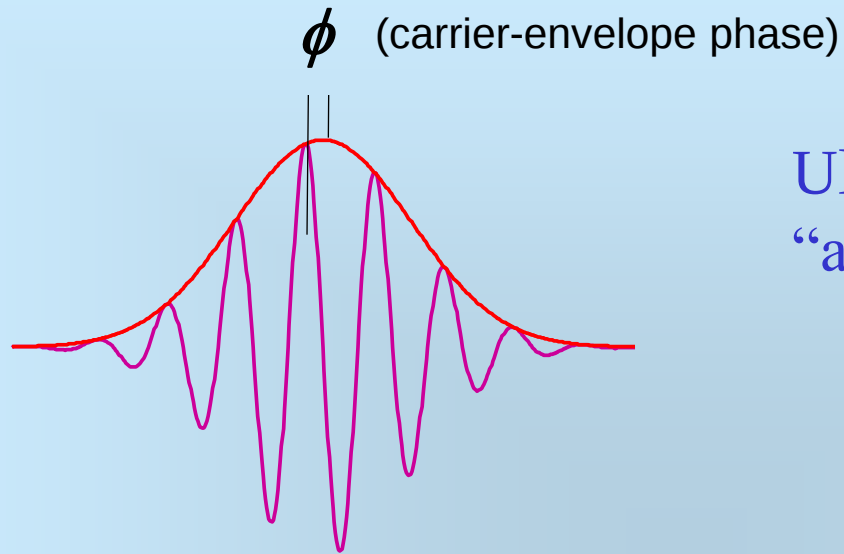
^{40}K Fermions



^{87}Rb Bosons



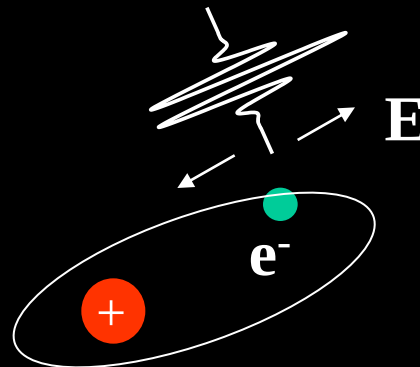
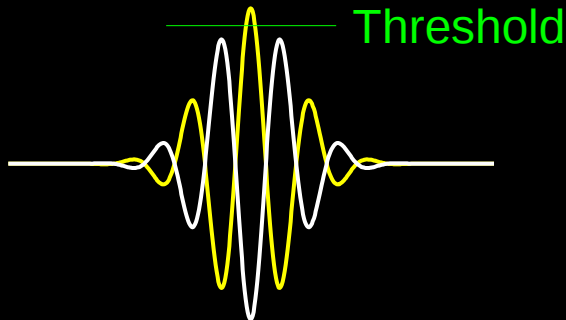
Phase-sensitive ultrafast science



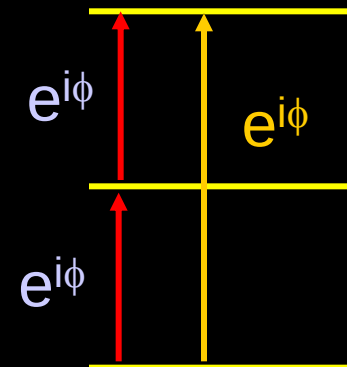
Ultra-short pulse provides
“absolute” phase reference

Processes sensitive to E-field
 (“extreme nonlinear optics”)

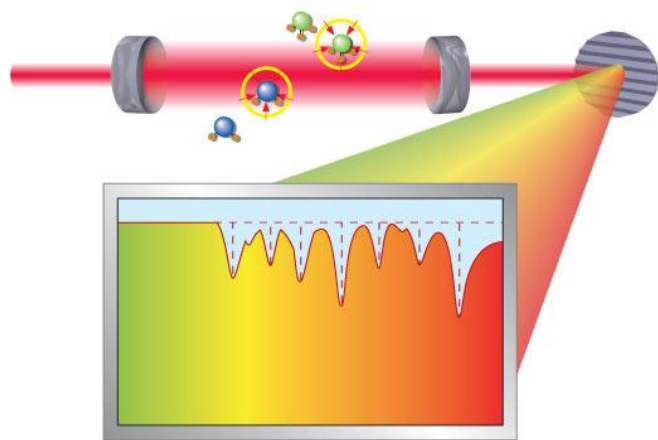
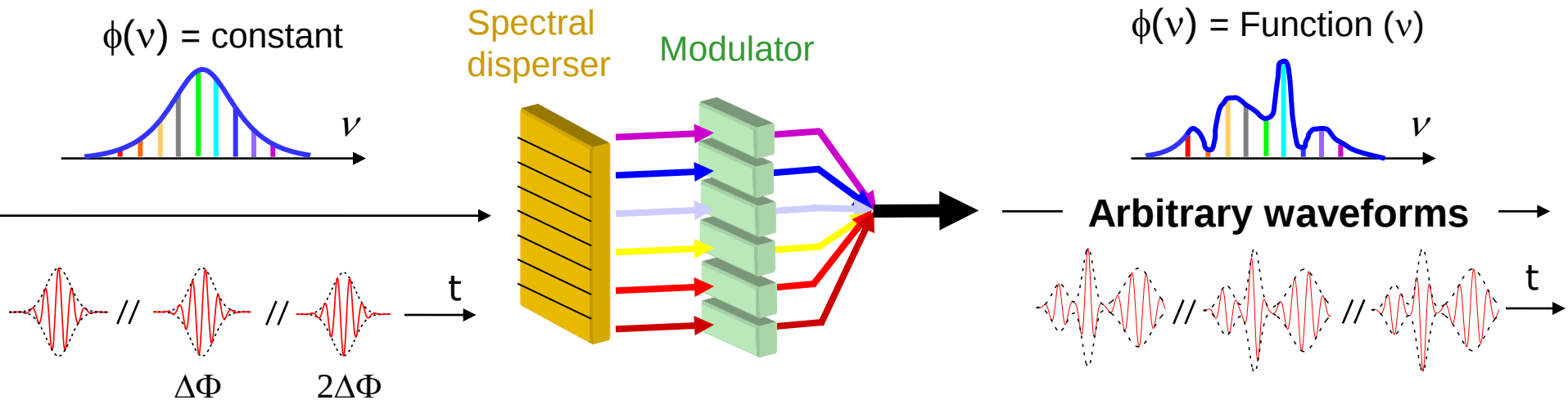
- Ionization & x-ray generation
- Tunneling from metal surface



Quantum interference
between perturbation orders

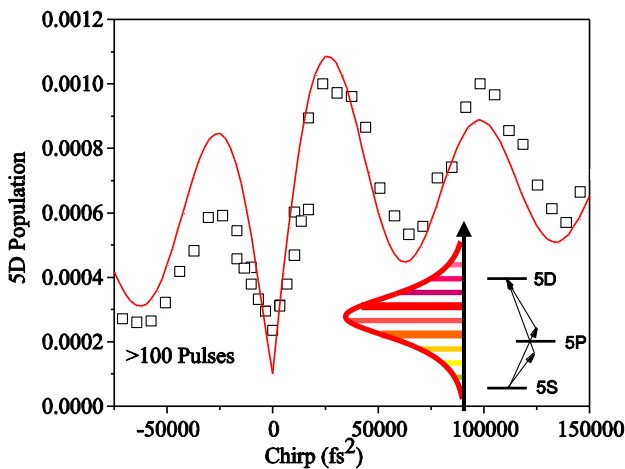


Optical Arbitrary Waveform Generation



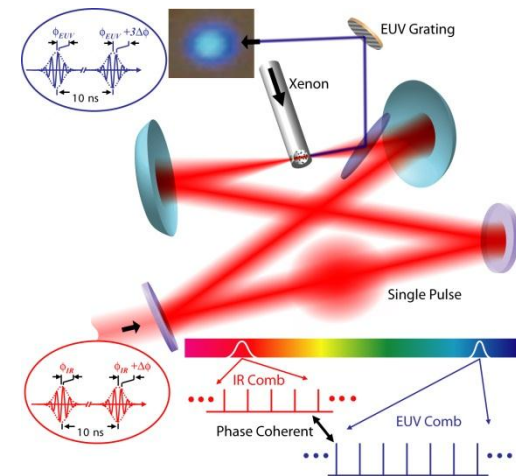
Molecular spectroscopy
(cold molecules)

Thorpe *et al.*,
Science **311**, 1595 (2006).



Quantum control

Stowe *et al.*,
PRL **96**, 153001(2006).
PRL **100**, 203001 (2008)



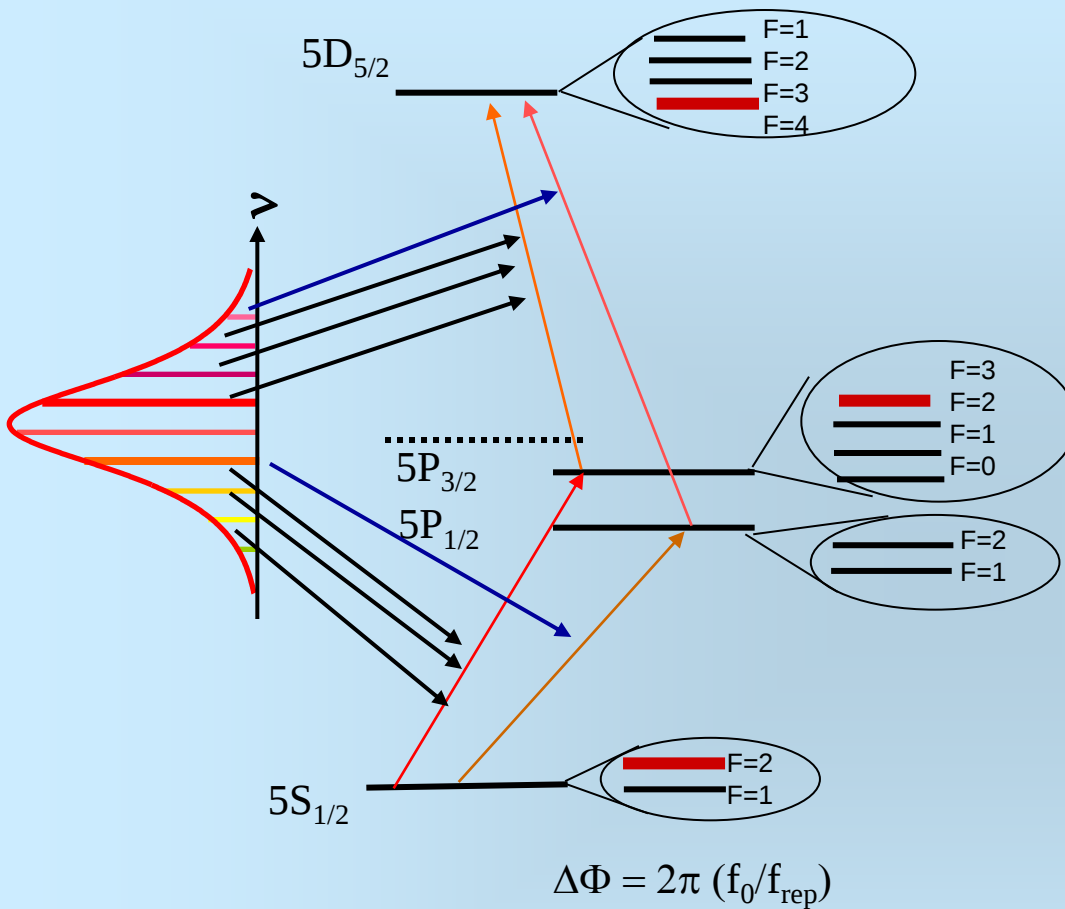
XUV comb

Jones *et al.*
PRL **94**, 193201 (2005).
C. Gohle *et al.*,
Nature **436**, 234 (2005).

Direct Frequency Comb Spectroscopy

Marian, Stowe, Lawall, Felinto, Ye
Science **306**, 2063 (2004).

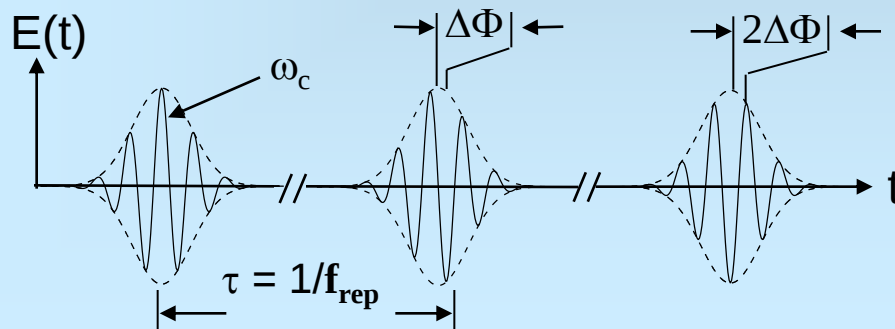
Stowe *et al.*,
PRL **96**, 153001 (2006).
PRL **100**, 203001 (2008).



Quantum & optical
coherence

High resolution
quantum control

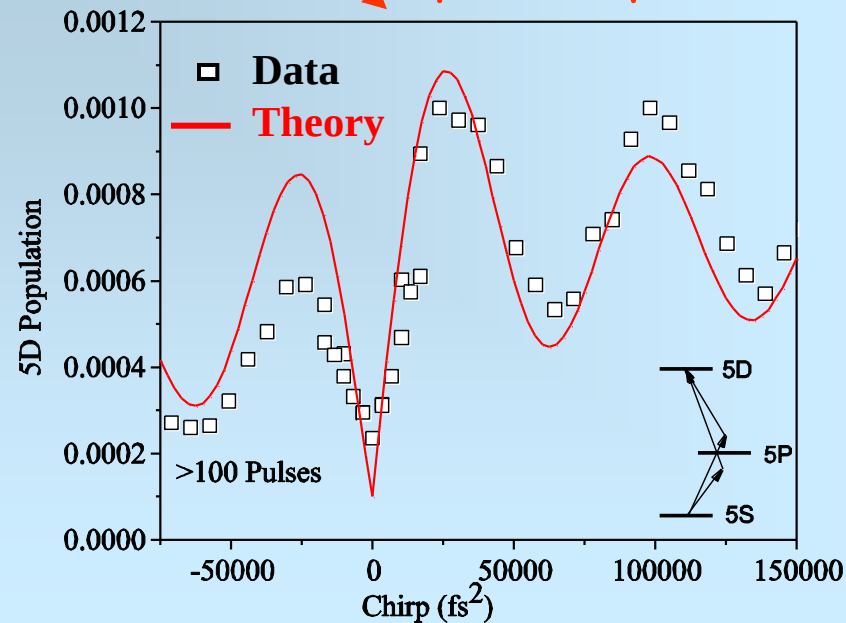
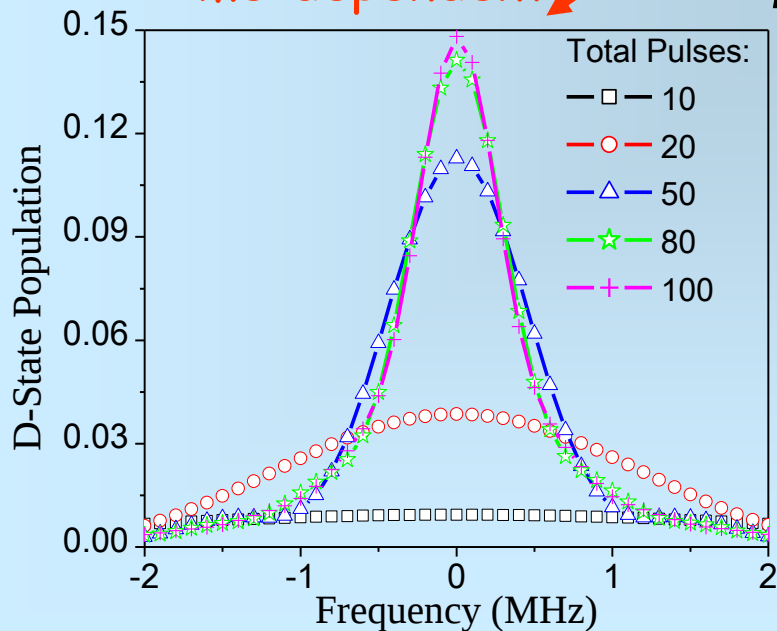
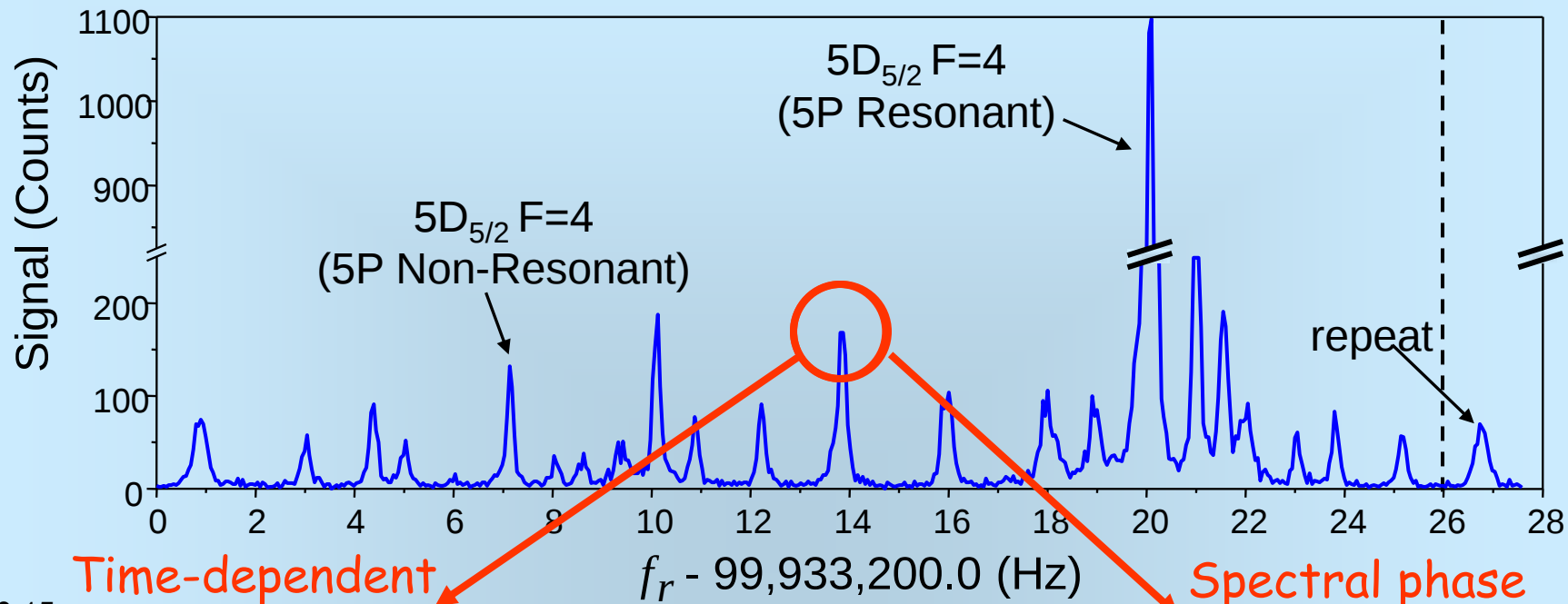
Precision spectroscopy:
global atomic structure



Ultracold Rb



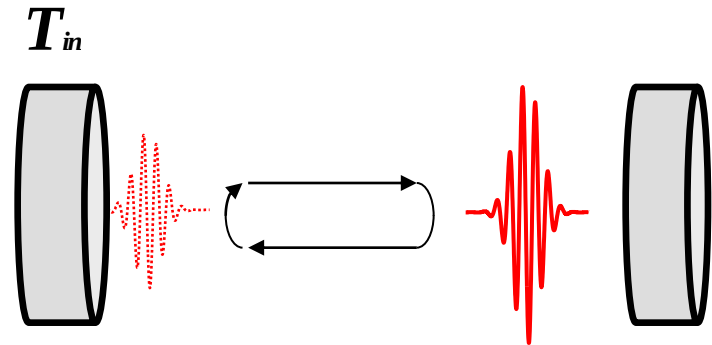
Global atomic structure & Control



Cavity - comb coherent coupling

Time Domain

J. Jones & Ye, Opt. Lett. 27, 1848 (2002)



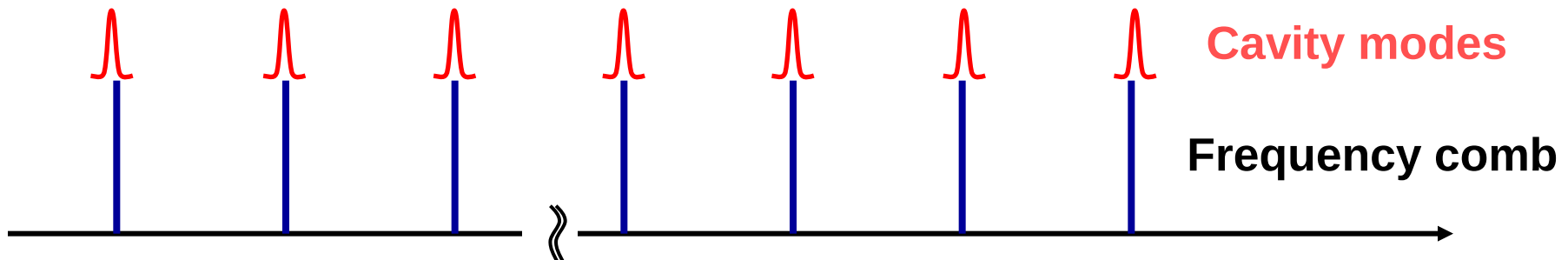
- Linear response
- Preserves coherence
- **Power & Length enhancement**

Cavity enhancement:

$$N = \frac{4T_{in}}{L^2} = 4T_{in} \left(\frac{F}{2\pi} \right)^2$$

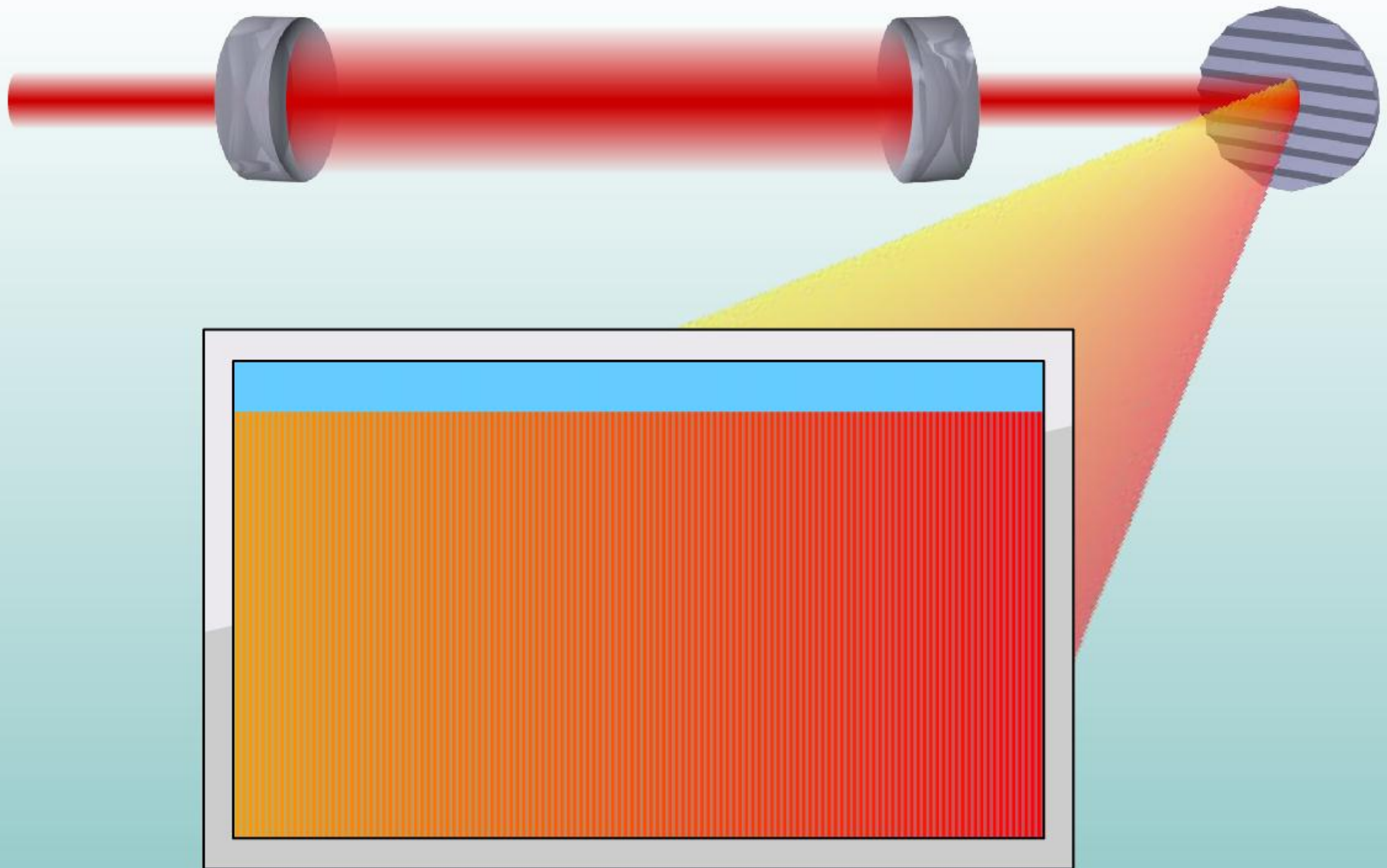
Frequency Domain

J. Jones *et al.*, Phys. Rev. A 69, 051803 (R) (2004)



Cavity-enhanced Direct Frequency Comb Spectroscopy

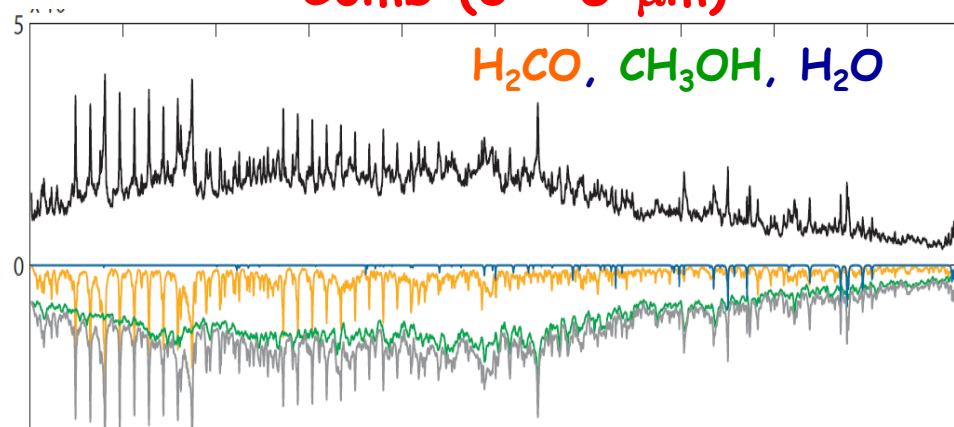
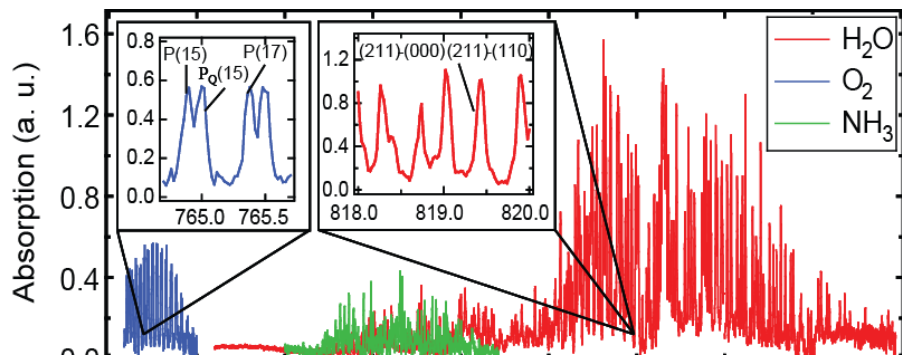
Thorpe et al., Science **311**, 1595 (2006).
Foltynowicz et al., PRL **107**, 233002 (2011).



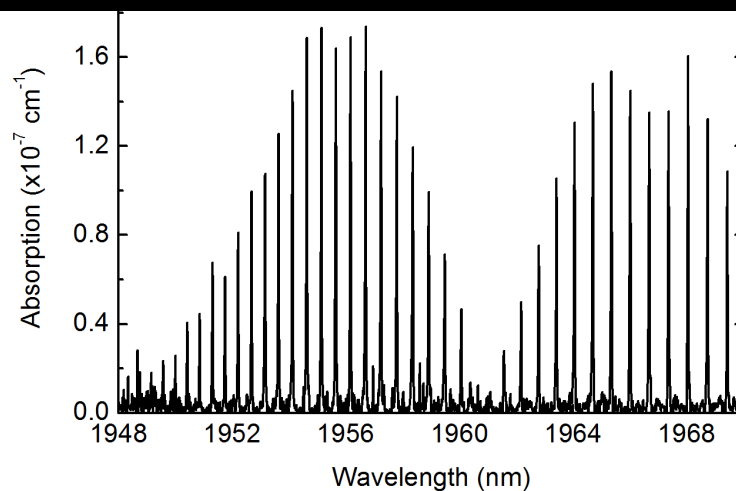
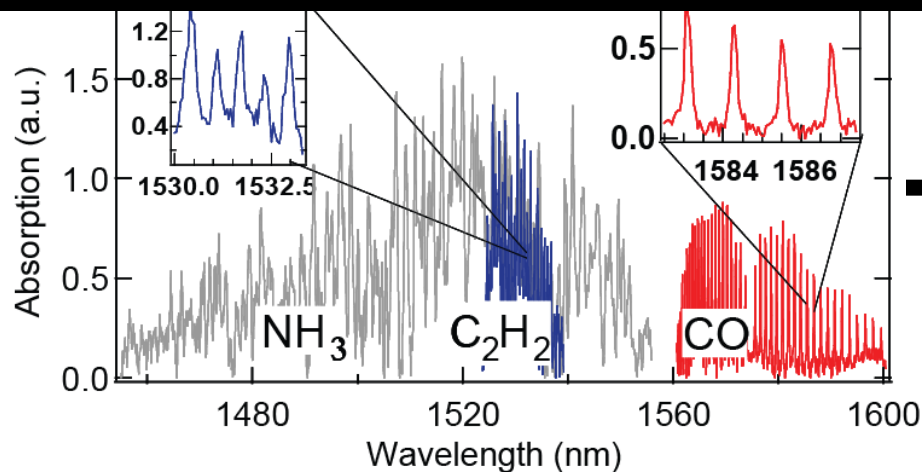
Wide spectral coverage

Comb (3 - 5 μm)

800 nm comb



- Broad spectral coverage
- High sensitivity ($1 \times 10^{-10} \text{ cm}^{-1}\text{Hz}^{-1/2}$; parts per 10^9)
- High resolution
- Real time acquisition



Application case: Breath analysis

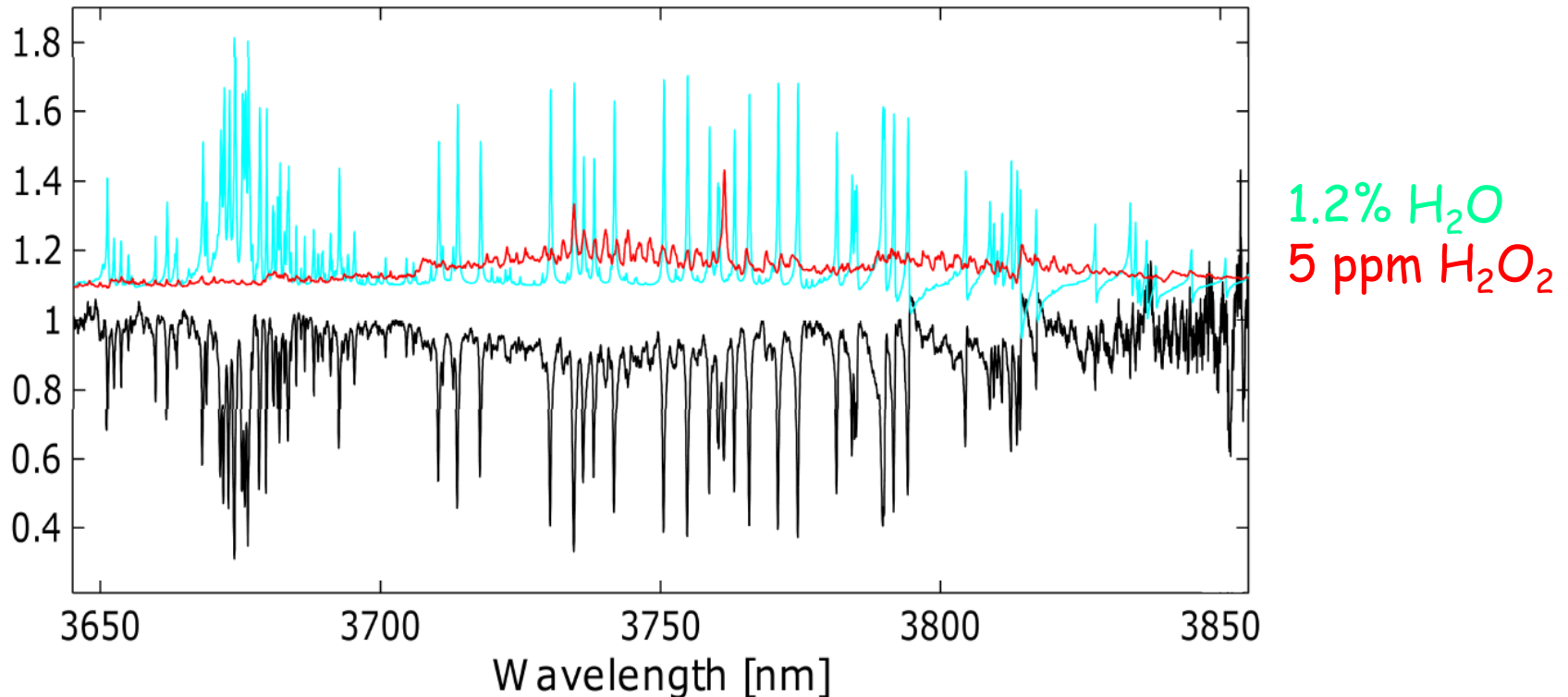
H_2O_2 : Marker of Acute Respiratory Distress Syndrome

Mortality: 30-40%

Elevated level of H_2O_2 in breath of ARDS cases: ~ 10 ppm

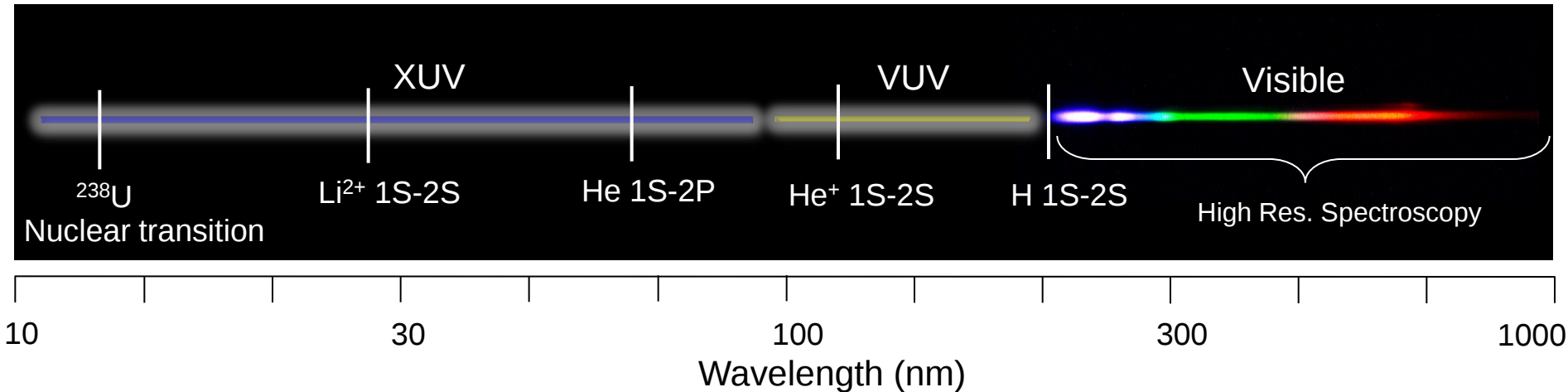
Dr. John Repine, Univ. Colo. Medical School, J. Pulmonar Respirat Med 2012.

Comb detection limit: 0.1 ppm



Foltynowicz et al., Appl. Phys. B, DOI 10.1007/s00340-012-5024-7 (2012).

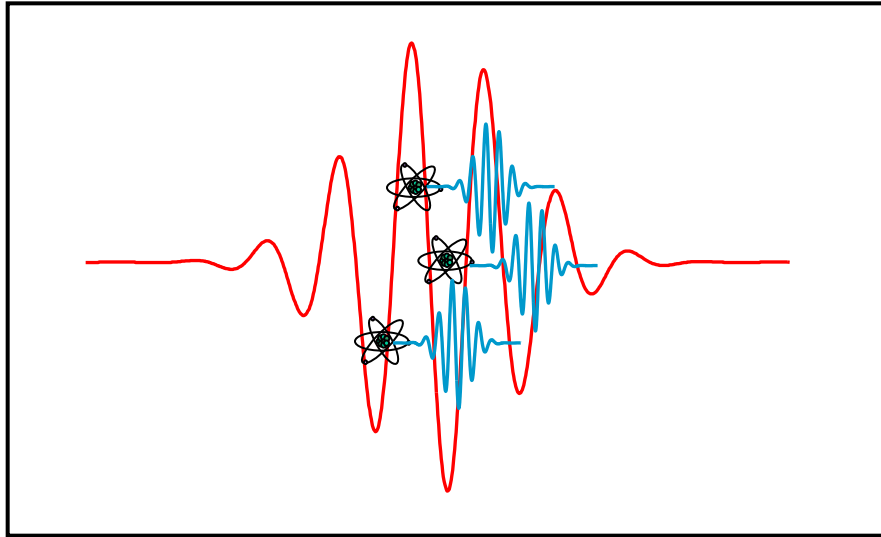
Charting the extreme ultraviolet landscape (Ultrahigh-resolution XUV spectroscopy)



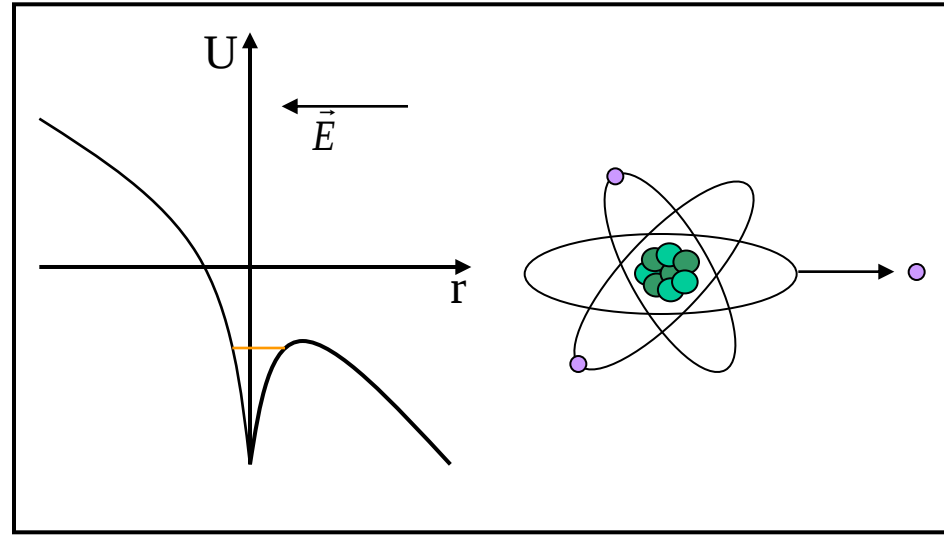
- Precision tests of fundamental physics
- Simple 3-body systems (i.e. helium), but also complex molecules
- Nuclear transitions
- High-precision test of QED
 - Ground state Lamb shift scales as Z^4
 - Higher-order corrections scale as Z^6

High-harmonic generation — VUV, EUV, soft X-ray

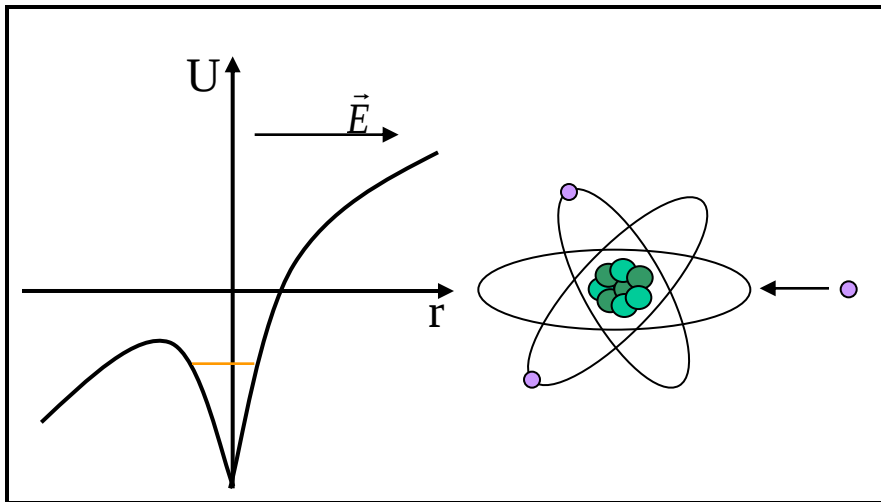
Three step model



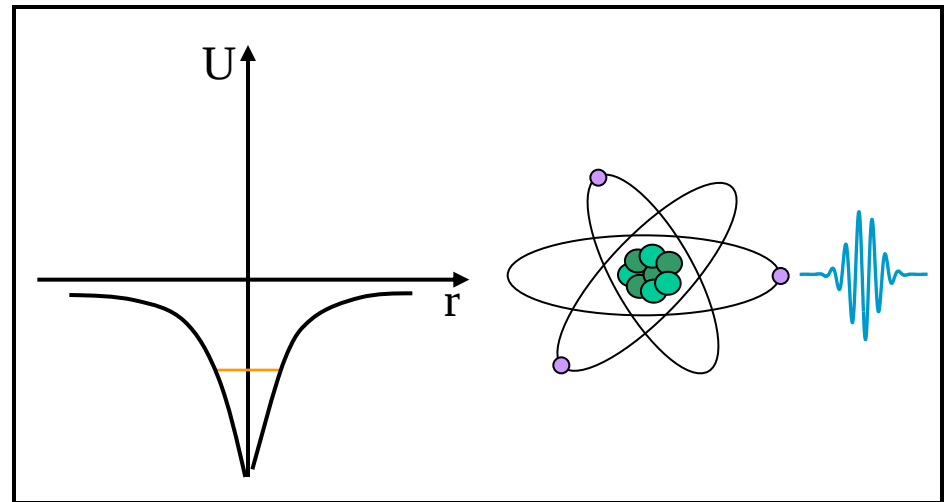
Step 1: Ionization



Step 2: Field Reversal



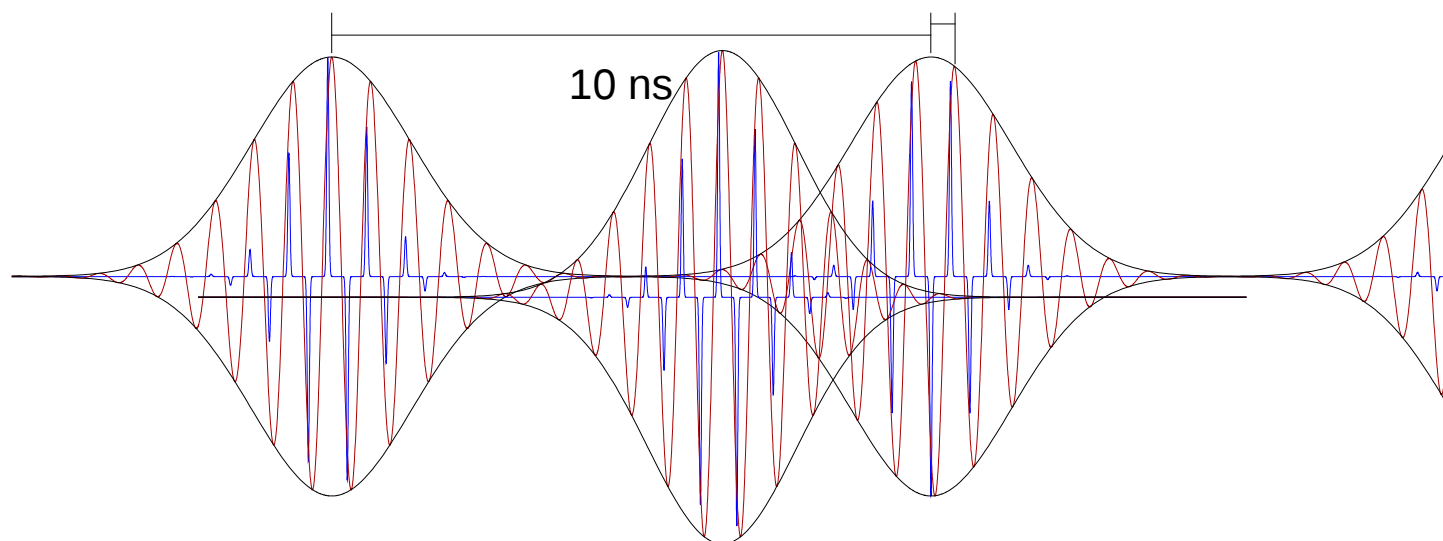
Step 3: Recombination



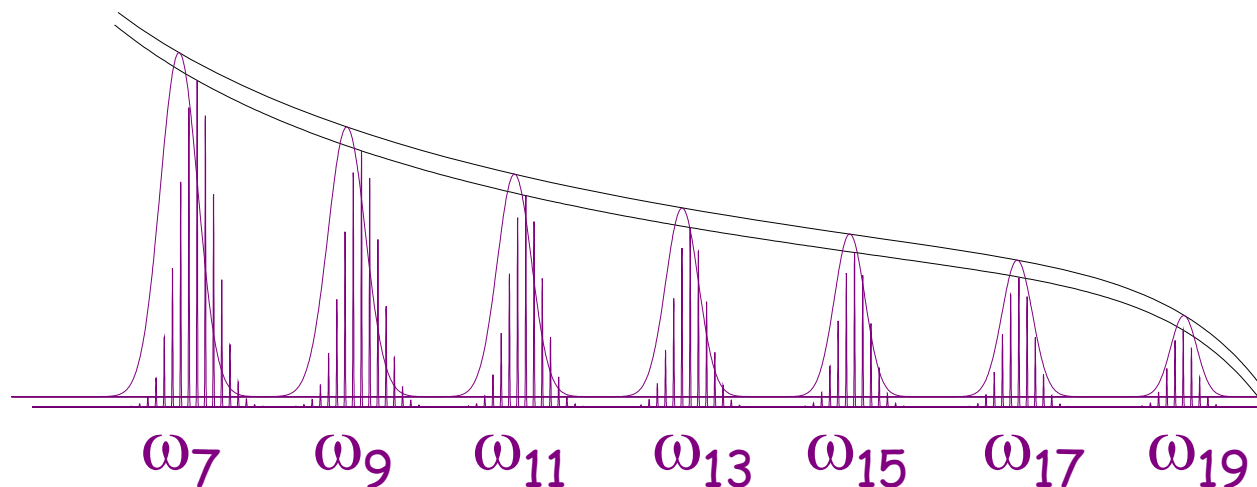
Coherent VUV and XUV radiation

Harmonic Generation with a train of IR pulses - a train of attosecond pulses
The XUV frequency comb is born

Time domain

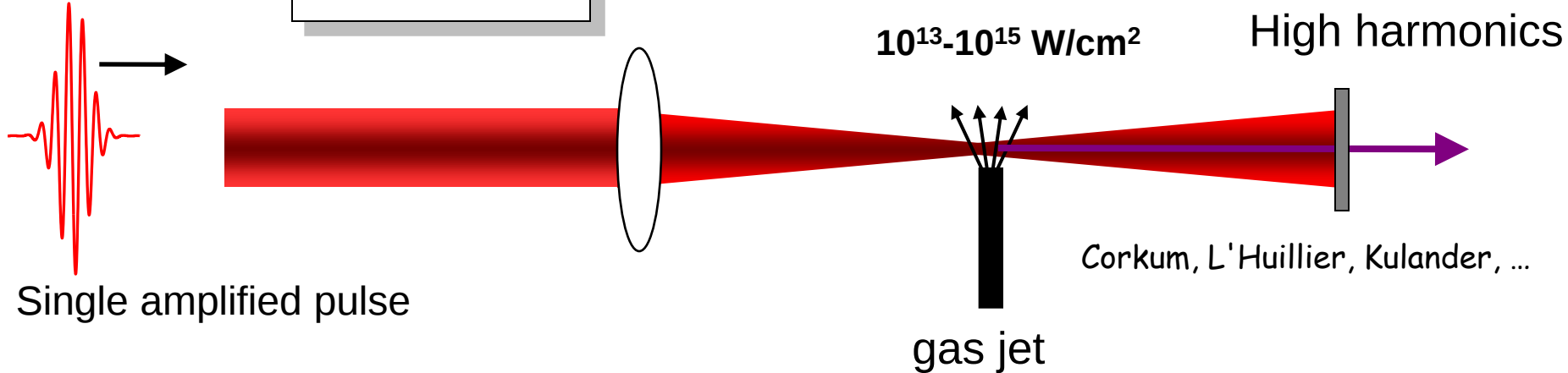


Frequency domain



High-harmonic generation

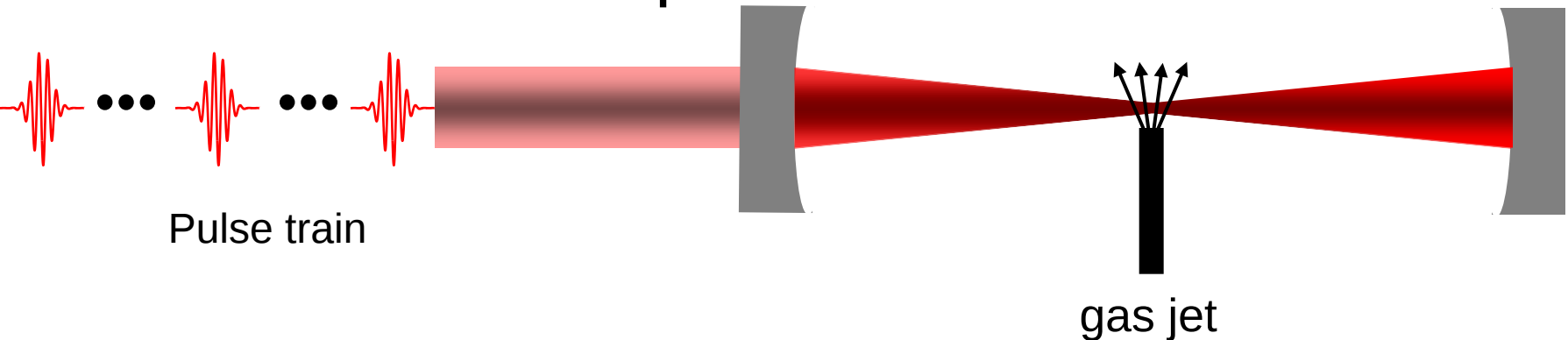
Single pass



fs enhancement cavity

Low repetition rates, (Hz ~ kHz)

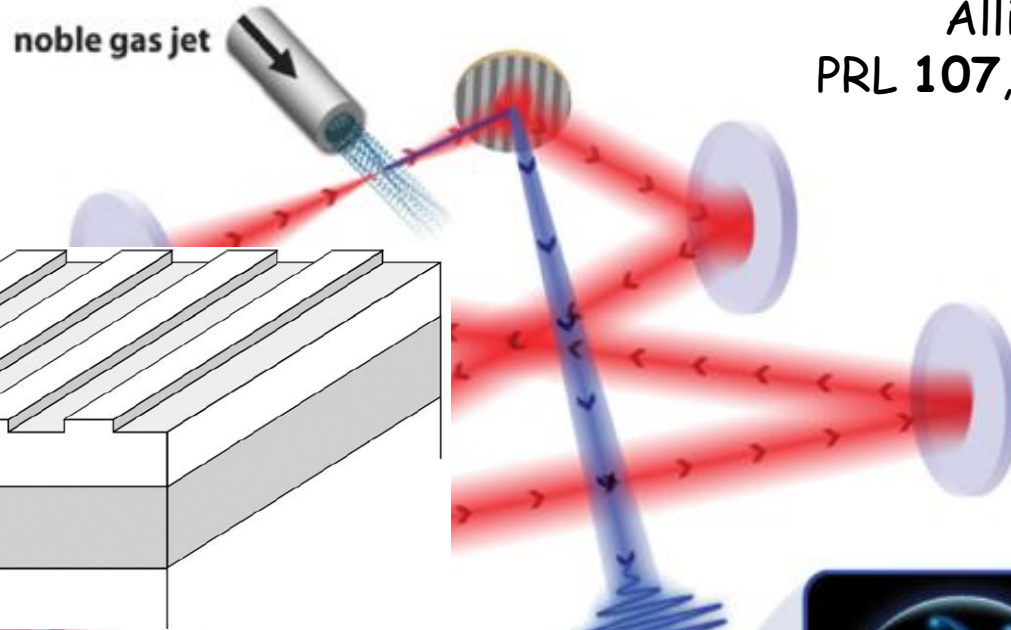
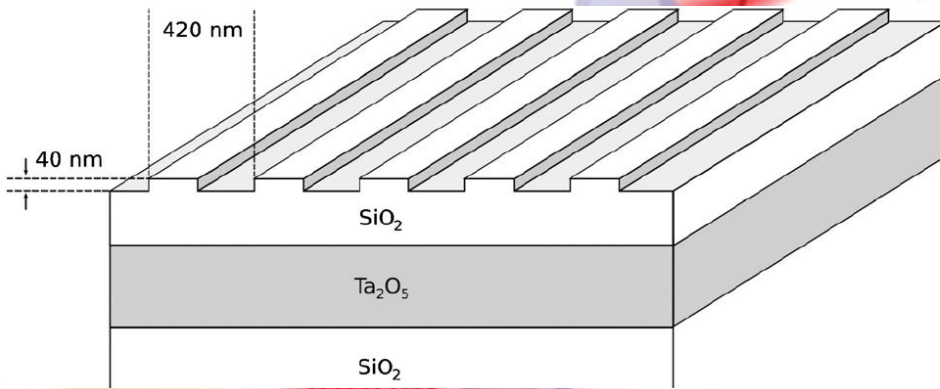
- Recycle unconverted energy
 - Maintain full repetition rate
- Conversion efficiency $10^{-5} \sim 10^{-8}$



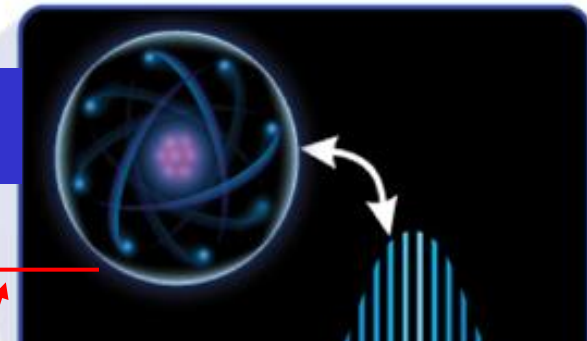
Power scaling - XUV frequency Comb

Allison et al.,
PRL 107, 183903 (2011).

Yost et al., Opt. Lett.
33, 1099 (2008)

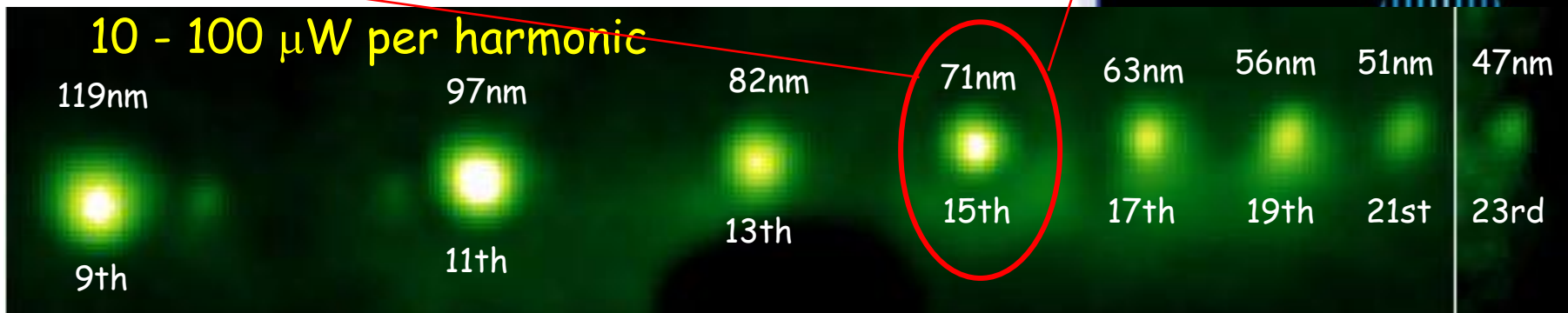


Does each HHG have its own comb ?



7th harmonic (152 nm) power > 1 mW !

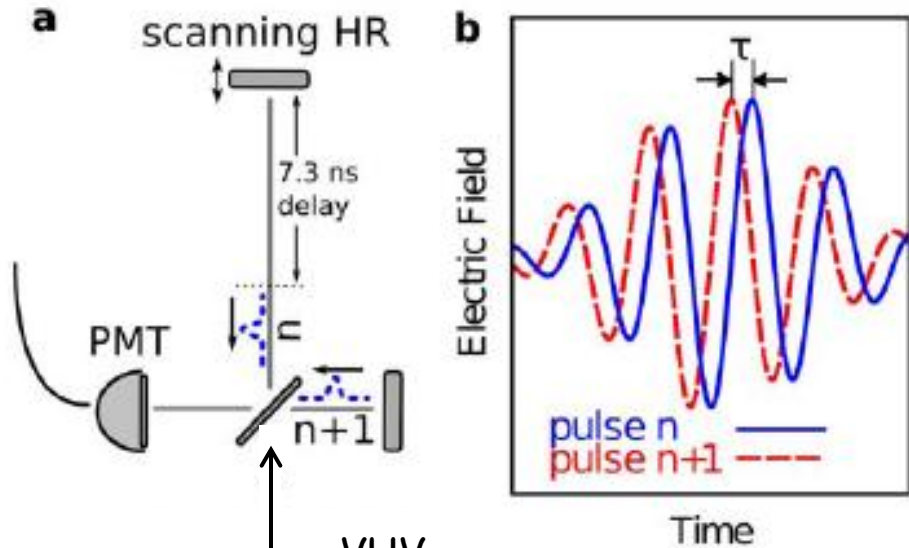
10 - 100 μ W per harmonic



Confirmation of VUV comb

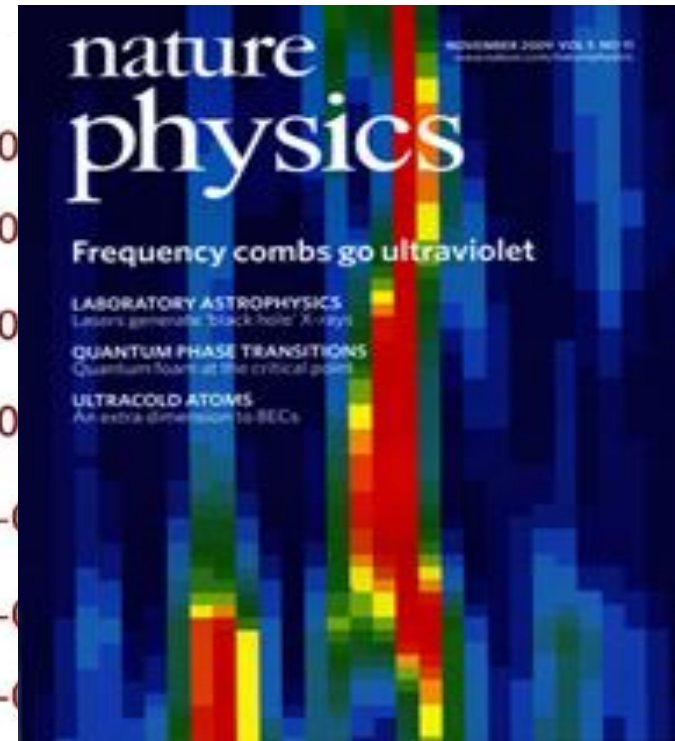
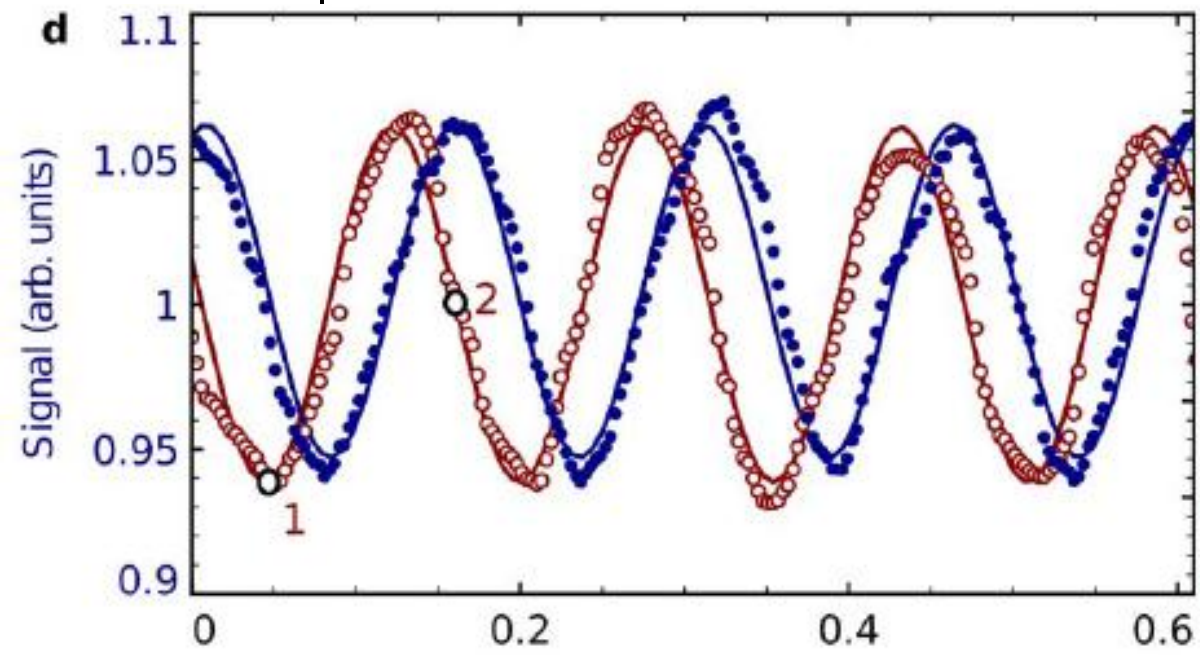
Yost et al., Nature Physics
5, 815 (2009).

VUV (7th harmonic)
comb linewidth
 ≤ 20 MHz



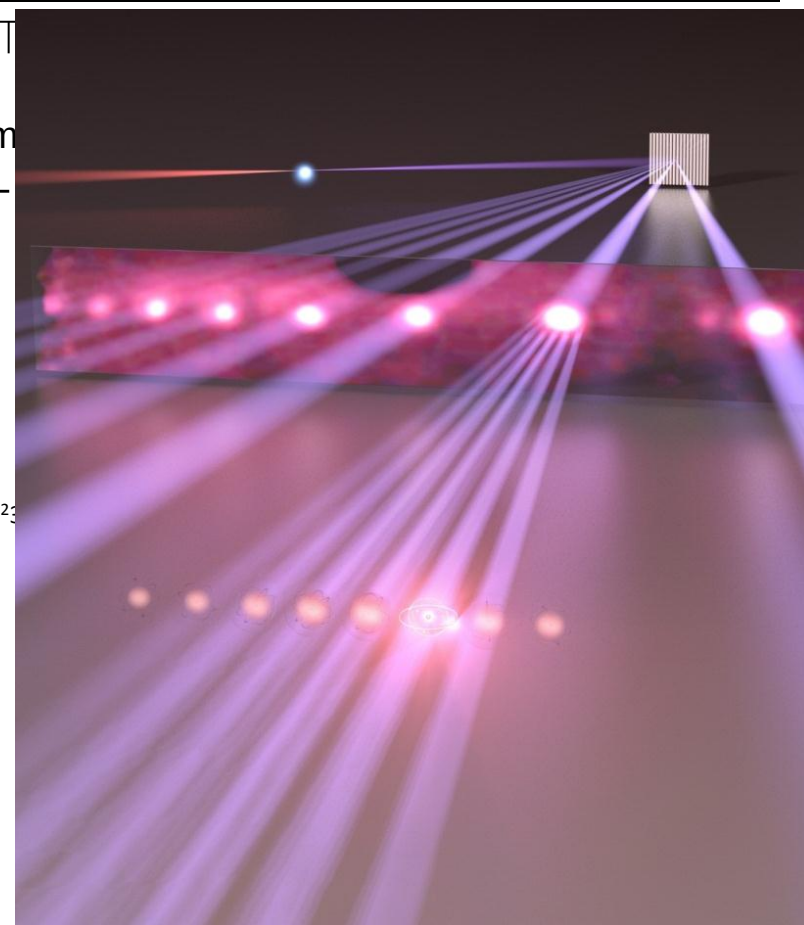
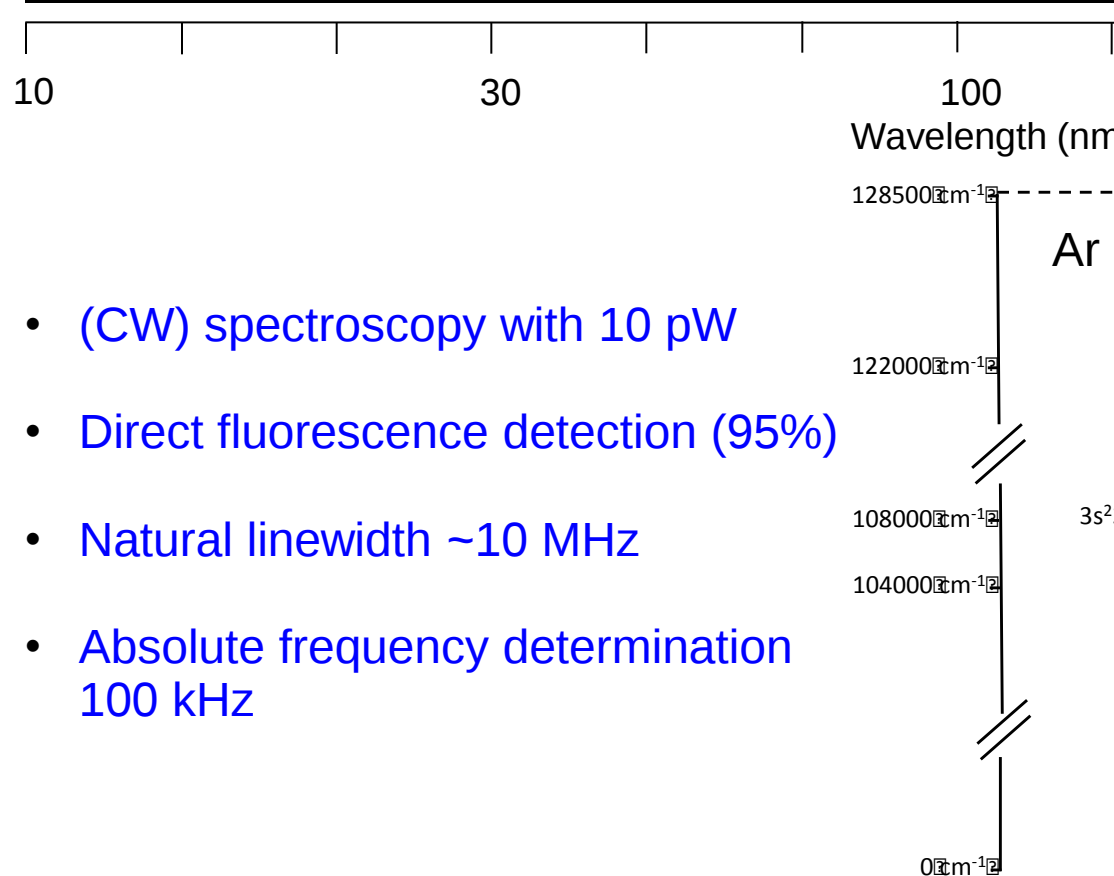
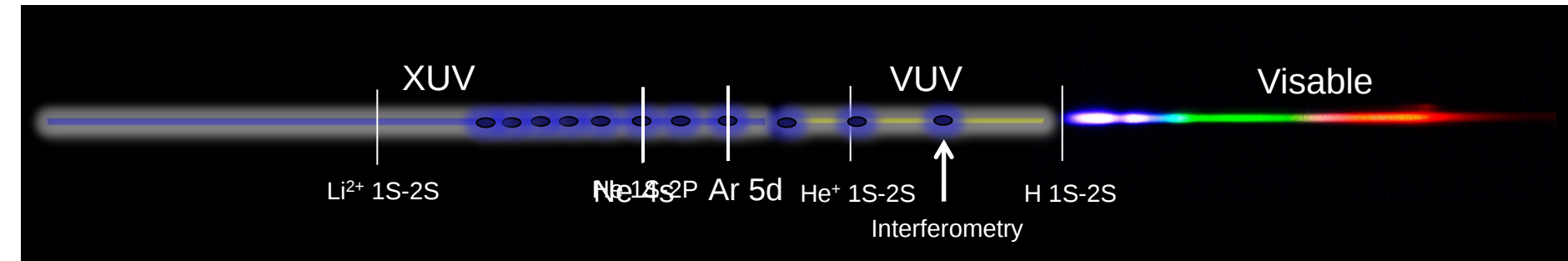
VUV
pulse train

A diagram showing a VUV pulse train. It consists of a series of blue pulses, with the first pulse labeled 'n'. A bracket indicates the duration of the pulse train.



Spectroscopy - the ultimate test

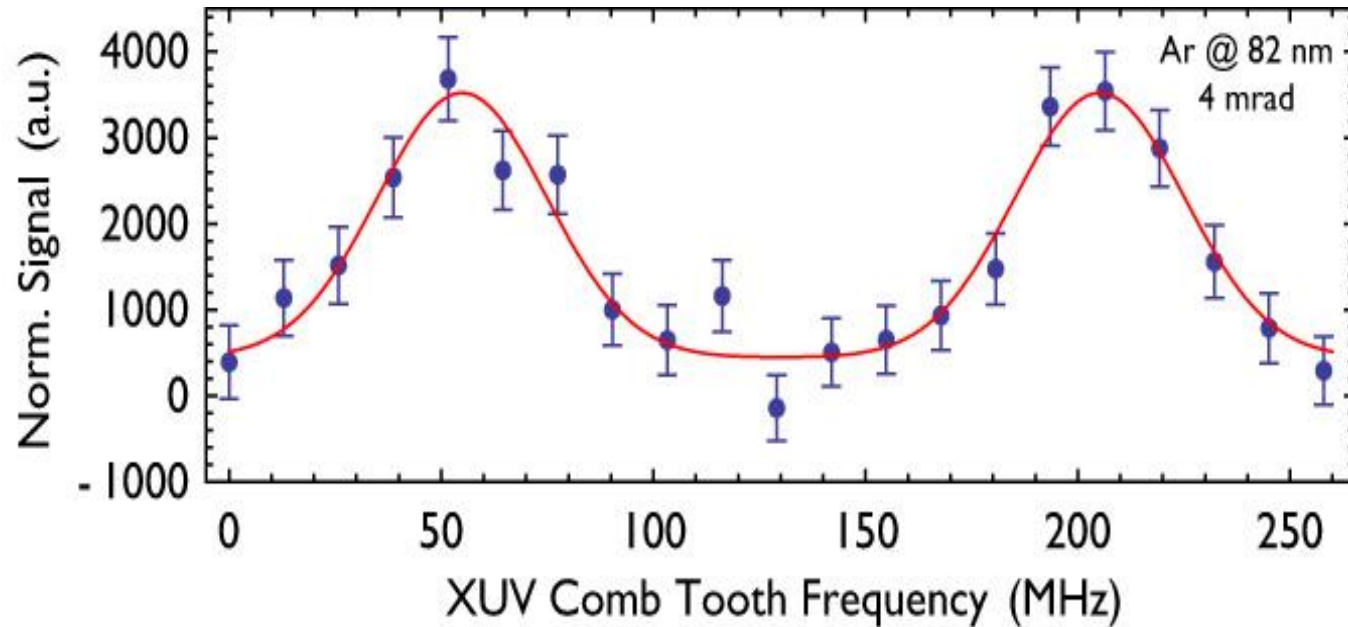
Cingöz et al., Nature 482, 68 (2012).



- (CW) spectroscopy with 10 pW
- Direct fluorescence detection (95%)
- Natural linewidth ~ 10 MHz
- Absolute frequency determination 100 kHz

Comb-Resolved Spectroscopy

Cingoz *et al.*, Nature 482, 68 (2012).



Scan a single comb
across resonance

Reduce the Doppler
broadening

Also,
Ne transition;
17th harmonic
(62 nm)

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