

Dynamic control of positional information in the early *Drosophila* embryo

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Morphogen gradients contribute to pattern formation by determining positional information in morphogenetic fields^{1,2}. Interpretation of positional information is thought to rely on direct, concentration-threshold-dependent mechanisms for establishing multiple differential domains of target gene expression^{1,3,4}. In *Drosophila*, maternal gradients establish the initial position of boundaries for zygotic gap gene expression, which in turn convey positional information to pair-rule and segment-polarity genes, the latter forming a segmental pre-pattern by the onset of gastrulation^{5–7}. Here we report, on the basis of quantitative gene expression data, substantial anterior shifts in the position of gap domains after their initial establishment. Using a data-driven mathematical modelling approach^{8–11}, we show that these shifts are based on a regulatory mechanism that relies on asymmetric gap–gap cross-repression and does not require the diffusion of gap proteins. Our analysis implies that the threshold-dependent interpretation of maternal morphogen concentration is not sufficient to determine shifting gap domain boundary positions, and suggests that establishing and interpreting positional information are not independent processes in the *Drosophila* blastoderm.

The maternal Bicoid (Bcd) gradient in blastoderm-stage embryos of *Drosophila melanogaster* is a classic example of a morphogen gradient^{12,13}. The modern morphogen concept⁴ implies that Bcd by itself should be able to specify directly the domain boundaries of its target genes, such as the gap genes *Krüppel* (*Kr*), *giant* (*gt*) (Fig. 1a), *knirps* (*kni*) and *hunchback* (*hb*) (Fig. 1b). Genetic and theoretical studies suggest, however, that gap gene regulation by Bcd requires regulatory synergism with maternal Hb^{9,14}, and quantitative experiments show that Bcd by itself cannot account for the precise positioning of zygotic *hb* expression^{12,15}. In addition, sharpening of gap domain boundaries and maintenance of gap gene expression rely on gap–gap cross-repression (see ref. 16, and references therein). It remains unclear, however, whether such cross-repression is required for correct positioning of gap gene boundaries, or if a combination of the maternal Bcd, Hb and Caudal (Cad) gradients is sufficient to determine positional information in the gap gene system.

Proof of the sufficiency of a given set of genetic interactions for specific expression patterns can be achieved only by reconstituting the underlying gene network from well-defined ingredients. Because this is currently impossible *in vitro*, we have used an *in silico* approach. The gene circuit method is a data-driven mathematical modelling approach for the computational reconstitution and

Box 1

The four steps of the gene circuit method

Step 1: Formulation of the model

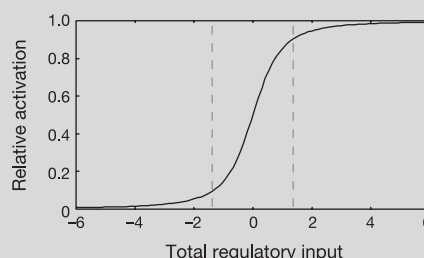
Gene circuits are hybrid dynamical models consisting of discrete nuclear divisions and continuous intranuclear dynamics of protein concentrations. Nuclei indexed by *i* are arranged in a one-dimensional row along the A–P axis, because A–P and D–V patterning systems are largely independent in the trunk region of the embryo. Gap gene circuit models cover 58 nuclei between 35 and 92% A–P position during cycles 13 and 14A²⁷, and include *bcd*, *cad*, *hb*, *Kr*, *kni*, *gt* and the terminal gap gene *tl*. The rates of change in protein concentration dv_i^a/dt for each regulated gene product *a* in each nucleus *i* during interphase are given by a system of 348 ordinary differential equations defined by

$$\frac{dv_i^a}{dt} = R_a g(u^a) + D^a [(v_{i-1}^a - v_i^a) + (v_{i+1}^a - v_i^a)] - \lambda_a v_i^a \quad (1)$$

The main terms on the right hand side of equation (1) represent protein synthesis, diffusion and decay respectively, with the corresponding rate parameters R_a , D^a and λ_a . Diffusion parameters are proportional to the inverse square distance between nuclei, which is halved on division. During mitosis, protein synthesis is shut down. Nuclear division occurs at the end of mitosis in cycle 13. $g(u^a)$ is a sigmoidal regulation–expression function, where u^a is given by

$$u^a = \sum_b T^{ab} v_i^b + m^a v_i^{\text{Bcd}} + h^a \quad (2)$$

For values of u^a below -1.5 and above $+1.5$, $g(u^a)$ rapidly approaches zero and one, respectively (broken lines in figure below).



Parameters T^{ab} constitute a genetic interconnectivity matrix and represent activation of gene *a* by the product of gene *b* if positive, repression if negative, and no interaction if close to zero. v_i^{Bcd} represents the concentration of Bcd in nucleus *i*, which is exclusively maternal and constant in time. m^a describes the regulatory input of Bcd to the zygotic system. Maternal contributions to Hb and Cad are represented as nonzero initial conditions. h^a represents regulatory input from ubiquitous maternal factors (see Supplementary Information for details).

Step 2: Quantitative gene expression data

Quantified expression profiles for products of genes *a* at one time point in cycle 13 and eight time points during cycle 14A are used for fits of the model to data (see Methods).

Step 3: Optimization to fit model to data

Parameter values are not fixed *a priori*, but are obtained by fitting the model to data. Numerically calculated model output is compared with quantitative gene expression data, and the difference between the two is minimized by adjusting parameter values using the PLSA optimization method (see Methods). In this way, we obtain specific sets of parameters, and thus specific gene circuits, which faithfully reproduce the expression patterns used for optimization (see Supplementary Information for parameter values).

Step 4: Biological analysis

Regulatory parameters of gene circuits contain information about the generative mechanism underlying the expression data used for optimization. We extract this information by graphical analysis of both the reaction and diffusion terms of equation (1), and the quantitative regulatory contributions $T^{ab} v_i^b$ by regulators *b* to specific genes *a* in each nucleus *i* in equation (2).

analysis of observed gene expression patterns, which allows us to infer regulatory interactions from wild-type gene expression data^{8–11,16} (Box 1).

Quantitative gene expression data show significant anterior shifts of gap domain boundaries during cleavage cycle 14A (Fig. 1c, e, g). Gap gene circuit models reproduce observed gap gene expression patterns, including boundary shifts of the central *Kr* domain and the posterior domains of *kni* and *gt*, with high precision and temporal resolution (Fig. 1d, f, h). Elsewhere, we have shown that our models also specifically and accurately reproduce the activation of gap genes by maternal factors and gap–gap cross-repression¹⁶. Taken together, this suggests that gap gene circuit models correctly represent the dynamic and genetic properties of the gap gene system.

In gap gene circuits, dynamic shifts of gap gene expression domains are reflected at the level of the rate of change in protein concentration (Fig. 2a–c). We can distinguish two discrete regulatory domains in the anterior and posterior portions of the *Kr*, *kni* and *gt* expression domains: protein synthesis dominates anteriorly, whereas protein decay posteriorly (Fig. 2d–f). The combination of anterior synthesis and posterior decay leads to an anterior shift of each expression domain. In addition, both the synthesis and decay domains themselves shift anteriorly over time (Fig. 2a–c).

The model thus predicts that synthesis is confined to the anterior region of each expression domain, implying that there is an asymmetric distribution of gap gene transcript in protein domains. Confirmation of this prediction is shown in Fig. 3. During cycle 14A, transcript domains of *Kr*, *kni* and *gt* are shifted anteriorly with respect to their corresponding protein domains (Fig. 3e–q). Such an asymmetrical distribution of *Kr* transcript and protein domains has been reported previously¹⁷, but it has not been interpreted in terms of dynamical shifts. In addition, anterior shifts of domain boundaries are present at both the transcript and the protein level (Fig. 3),

consistent with shifts in domains of synthesis, as observed in gene circuits (Fig. 2a–c).

A generative mechanism for gap domain shifts must explain the dynamic positioning of the domains of protein production and decay. Theoretically, shifts in domain boundaries can be caused by mechanisms based on gene regulatory interactions and/or the diffusion of gene products between neighbouring nuclei. In the syncytial blastoderm of *Drosophila*, the absence of cell membranes between nuclei allows the diffusion of gap gene products, leading to protein domains that, in general, are slightly larger than their corresponding transcript domains (Fig. 3).

Gene circuits allow us to examine the roles of regulatory and diffusive mechanisms by plotting the corresponding terms in the gene circuit equation (Box 1). Here, we illustrate our analysis with the example of the posterior boundary of *kni*. We compare temporal changes in protein concentration (Fig. 4a–c) to temporal changes in the reaction (protein synthesis and decay) and the diffusion terms of the equation (Fig. 4e–g). Nuclei that lie in the zone of the anterior shift of the posterior *kni* boundary show a characteristic switch from synthesis to decay of *Kni* protein during cycle 14A (Fig. 4a–c). This dynamical behaviour is directly responsible for the observed anterior shift of the boundary. It is closely mirrored by changes in the reaction terms of the equation, whereas diffusion leads to an influx of protein into the shift zone counteracting the boundary shift (Fig. 4e–g). For shifts in posterior borders, a counteracting role of diffusion is expected because the shift occurs toward increasing protein concentration in the boundary. But even for shifts in anterior boundaries, which occur in the direction of lower concentration, diffusion is not essential because these shifts are still present in gap gene circuits in which diffusion is not allowed to occur (see Supplementary Information). Thus, our analysis suggests that although gap protein diffusion is present in both embryo and gap gene circuits, it does not have a significant role in shifting gap domain boundaries.

Gene circuits allow us to study gene regulatory interactions by plotting combinations of regulatory contributions to the expression of a particular gene. For the shift in the posterior boundary of *kni*, we have found the following relevant regulatory contributions (Fig. 4i–k). Expression of *kni* is repressed in nuclei in the shift zone by spatially specific repressive inputs that counteract broad *Cad* activation throughout the posterior region of the embryo (Fig. 4i–k). Downregulation of *kni* in the posterior portion of the

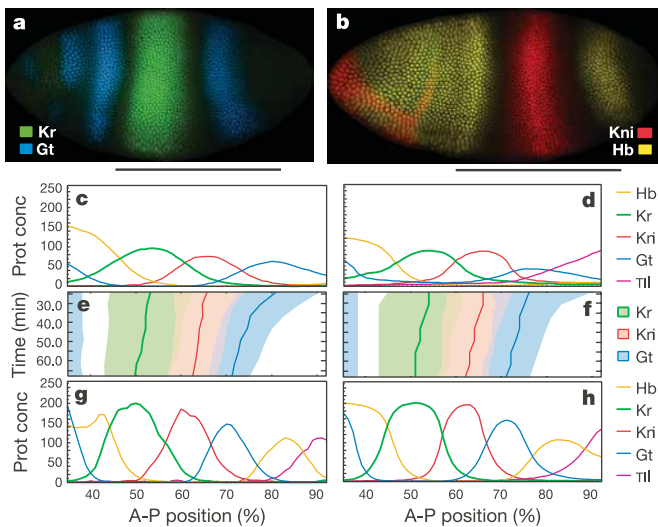


Figure 1 Dynamical shifts in gap gene domains are reproduced by gap gene circuits. **a, b**, *Drosophila melanogaster* blastoderm stage embryos at late cleavage cycle 14A (time class T8) immunostained for *Kr* and *Gt* (FlyEx embryo, *rge9*; **a**) and *Kni* and *Hb* (*rb8*; **b**). Anterior is to the left, dorsal is up. Bars indicate the region included in gap gene circuits. **c, d, g, h**, Gene expression data (**c, g**) and gap gene circuit model output (**d, h**) at early (T1; **c, d**) and late (T8; **g, h**) cycle 14A. Vertical axes represent relative protein concentrations, horizontal axes represent position along the A–P axis (where 0% is the anterior pole). There are no T1 data for T1 (**c**). **e, f**, Gap domain shifts for *Kr*, *kni* and *gt* covering the time between patterns shown in **c, d** and **g, h**. Lines indicate the position of maximum concentration for each domain. Coloured areas represent regions in which protein concentration is above the half-maximum value. Positional values for data were obtained by approximation with quadratic splines²².

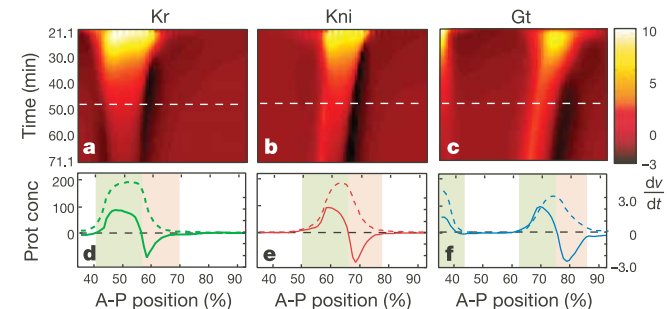
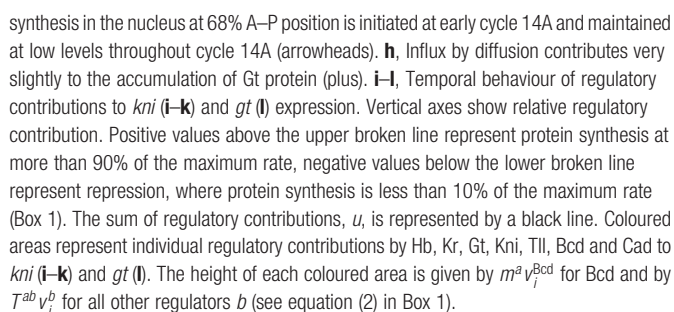
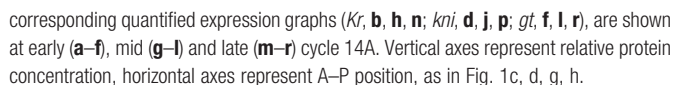


Figure 2 Shifting domains of gap protein synthesis and decay. **a–c**, Time–space diagrams, based on model output, of rate of change in protein concentration, dv/dt , for *Kr* (**a**), *Kni* (**b**) and *Gt* (**c**) during cycle 14A. Vertical axes represent time, horizontal axes represent position along the A–P axis. Note the shifting positions of domains of protein synthesis (yellow, light red) and protein decay (black). **d–f**, Cross-sections through **a–c** at time class T5 (broken white lines in **a–c**) for *Kr* (**d**), *Kni* (**e**) and *Gt* (**f**). Broken lines represent relative protein concentration, solid lines represent the rate of change in protein concentration, dv/dt . Domains of protein synthesis and decay are indicated by the light green and red backgrounds, respectively.

By contrast, more anterior nuclei show high levels of Kni synthesis in the absence of any significant repression (Fig. 4i). The



increasing Kni synthesis in the anterior portion of the shift zone is largely caused by stably maintained Kni autoactivation (Fig. 4i). More posterior nuclei do not reach the threshold concentration of Kni required for stable maintenance of autoactivation and show only moderate transient (Fig. 4j) or no (Fig. 4k) Kni autoactivation. Localized autoactivation is a consequence of the asymmetric repressive mechanism described above, rather than a cause of shifting domain boundaries. This is corroborated by the fact that a gap gene circuit without *kni* autoactivation shows correct shifts of *kni* domain boundaries (see Supplementary Information).

We have also analysed shifts of other gap gene domain boundaries (see Supplementary Information). With the exception of the posterior boundaries of the anterior *hb* and *gt* domains, we have detected anterior shifts in all boundaries examined (Fig. 1c–h). The shifts of the posterior boundaries of *Kr* and posterior *gt* are caused by asymmetric repressive interactions between *Kr* and *kni*, and *gt* and *hb*, very similar to those described for *kni*. Posterior dominance of repressive interactions among neighbouring gap genes is reminiscent of homeotic gene regulation, where posterior homeotic genes repress more anterior ones, but not vice versa¹⁸. Shifts of anterior gap domain boundaries either follow the posterior boundary shifts of more anterior gap genes or are due to sharpening of the posterior boundaries of anterior *gt* and *hb*. For example, the upregulation of *gt* in nuclei anterior to its posterior expression domain follows diminished repression by *Kr* (Fig. 4l). Therefore, shifts of anterior gap domain boundaries can be considered to be secondary effects of the dynamic behaviour of posterior boundaries.

Our results indicate that maternal Bcd, Hb and Cad alone are not sufficient for positioning of gap gene domains and hence do not qualify as morphogens in a strict sense. As has been pointed out¹⁹, an active role of target tissue in specifying positional information contradicts the traditional distinction between the instructive role of maternal morphogens and their passive interpretation¹. The requirement of specific regulatory interactions in the target tissue for proper interpretation of positional information can be interpreted as a requirement for specific tissue competence²⁰. In addition, the dynamical nature of positional information, as encoded by expression boundaries, suggests that positional information in the blastoderm embryo can no longer be seen as a static coordinate system imposed on the embryo by maternal morphogens¹. Rather, it needs to be understood as the dynamic process underlying the positioning of expression domain boundaries, which is based on both external inputs by morphogens and tissue-internal feedback among target genes. □

Methods

Acquisition of quantitative data

Drosophila blastoderm embryos were immunostained for three segmentation gene products each²¹. Each embryo was stained for Even-skipped (Eve) protein for time classification and registration²². We scanned laterally oriented embryos by laser confocal microscopy. Scanned images were aligned along the anteroposterior (A–P) axis and segmented by using binary nuclear masks to yield per-nucleus expression data for each protein.

Processing of quantitative data

Embryos were classified temporally as belonging to cycles 12 (for initial conditions), 13, or eight equally distributed time classes (T1–T8) in cycle 14A. Temporal classification in cycle 14A is based on the highly dynamic expression pattern of *eve*²². Expression patterns were registered by using a fast dyadic wavelet transform²². We removed nonspecific background staining. Data from the middle 10% of dorsoventral (D–V) positional values of each embryo were averaged for each gene and time class to yield an integrated data set that currently contains data based on 954 embryos, available in the FlyEx Database (<http://urchin.spbcas.ru/flyex>).

RNA/protein double staining

RNA was detected using digoxigenin-labelled RNA probes²³. RNA hybridization was done before protein detection by using standard protocols with the exception of permeabilization, where Proteinase K was replaced by acetone treatment²⁴. We obtained quantified expression profiles by image segmentation as described above.

Numerical simulations

Simulator and optimizer code was implemented in C, Java and Perl and is available on the Reinitz Lab website (<http://flyex.ams.sunysb.edu/lab/gaps.html>). Ordinary differential equations were solved numerically by using a Bulirsch–Stoer adaptive step size method²⁵. Integration was done to 0.1% accuracy, and the stability of solutions was confirmed.

Optimization

The sum of squared differences between model and data was minimized using parallel Lam simulated annealing (PLSA)^{10,26}. Search spaces were defined by explicit limits as well as a penalty function¹⁰. Each optimization run was done in parallel on ten 2.4-GHz Pentium P4 Xeon processors and took between 8 and 160 h per gene circuit.

Gene circuit selection and analysis

Because PLSA is a stochastic method, the quality of the resulting gene circuits can vary. Best solutions were selected as described elsewhere¹⁶. The selection process yielded 10 circuits (out of 40), which were used in the present analysis (see Supplementary Information). These circuits show strong constraints toward a specific gap gene network topology¹⁶. All data shown here are based on one particular gap gene circuit that shows no visible patterning defects and corresponds exactly to the network topology observed in most selected circuits.

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